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## Programming Languages

Title: Petter: Programmiersprachenh  
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Mixins and Traits

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### Outline



#### Design Problems

- 1 Inheritance vs Aggregation
- 2 (De-)Composition Problems

#### Cons of Implementation Inheritance

- 1 Lack of finegrained Control
- 2 Inappropriate Hierarchies

#### Inheritance in Detail

- 1 A Model for single inheritance
- 2 Inheritance Calculus with Inheritance Expressions
- 3 Modeling Mixins

#### A Focus on Traits

- 1 Separation of Composition and Modeling
- 2 Trait Calculus

#### Mixins in Languages

- 1 Simulating Mixins
- 2 Native Mixins

#### Traits in Languages

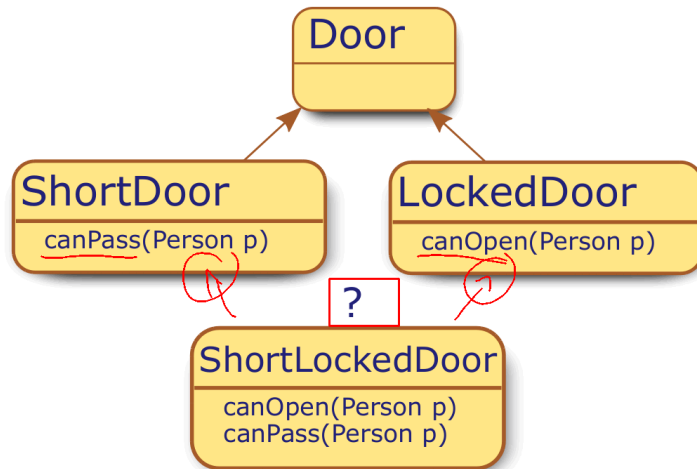
- 1 (Virtual) Extension Methods
- 2 Squeak

### Reusability $\equiv$ Inheritance?

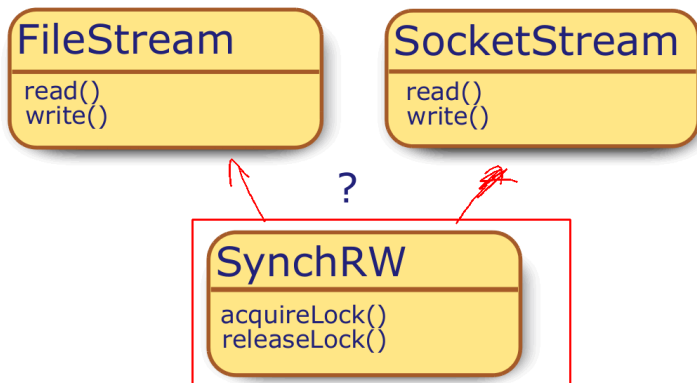


- Codesharing in Object Oriented Systems is often inheritance-centric
- Inheritance itself comes in different flavours:
  - single inheritance
  - multiple inheritance
- All flavours of inheritance tackle problems of *decomposition* and *composition*

## The Adventure Game



## The Wrapper

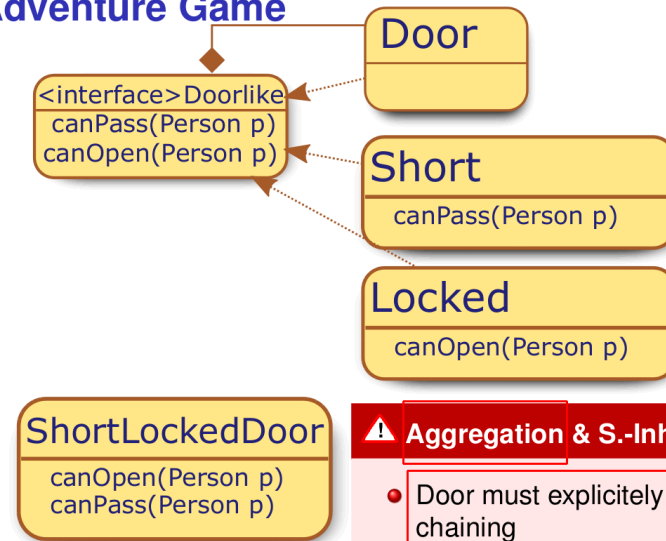


### ⚠️ Unclear relations

↪ Cannot inherit from both in turn with Multiple Inheritance  
(*Many-to-One* instead of *One-to-Many* Relation)



## The Adventure Game



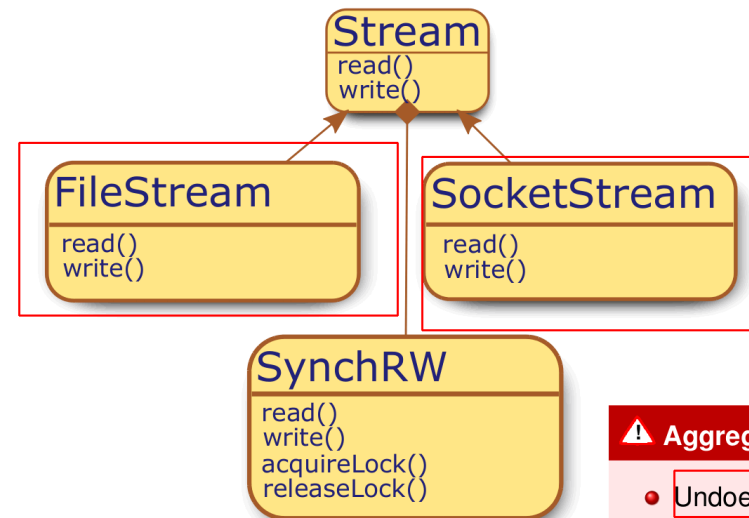
### ⚠️ Aggregation & S.-Inheritance

- Door must explicitly provide chaining
- Doorlike must anticipate wrappers

⇒ Multiple Inheritance ✓



## The Wrapper – Aggregation Solution

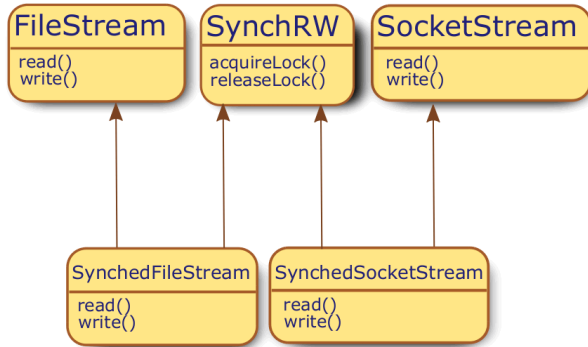


### ⚠️ Aggregation

- Undoes specialization
- Needs common ancestor



# The Wrapper – Multiple Inheritance Solution



## ⚠ Duplication

With multiple inheritance, read/write Code is essentially *identical but duplicated for each particular wrapper*

# (De-)Composition Problems



All the problems of

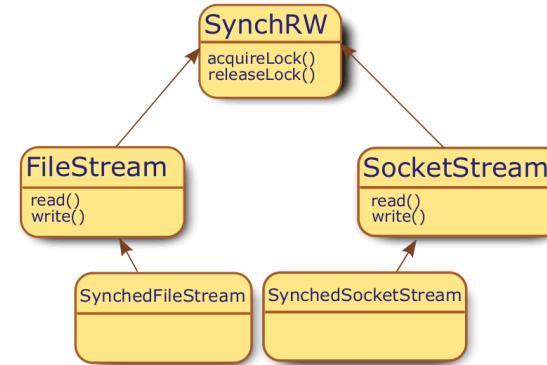
- Relation
- Duplication
- Hierarchy

are centered around the question

“How do I distribute functionality over a hierarchy”

↪ *functional (de-)composition*

# Fragility



## ⚠ Inappropriate Hierarchies

Implemented methods (acquireLock/releaseLock) *to high*

# Classes and Methods



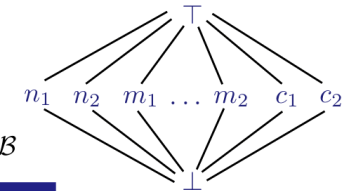
The building blocks for classes are

- a countable set of method *names*  $\mathcal{N}$
- a countable set of method *bodies*  $\mathbb{B}$

Classes map names to elements from the *flat lattice*  $\mathcal{B}$  (called bindings), consisting of:

- $\perp$  *method bodies*  $\in \mathbb{B}$  or *classes*  $\in \mathcal{C}$
- $\perp$  *abstract*
- $\top$  *in conflict*

and the partial order  $\perp \sqsubseteq b \sqsubseteq \top$  for each  $b \in \mathcal{B}$



## Definition (Abstract Class $\in \mathcal{C}$ )

A general function  $c : \mathcal{N} \mapsto \mathcal{B}$  is called a class.

## Definition (Interface and Class)

A class  $c$  is called (with pre being the preimage)

- interface* iff  $\forall n \in \text{pre}(c) . c(n) = \perp$ .
- abstract class* iff  $\exists n \in \text{pre}(c) . c(n) = \perp$ .
- concrete class* iff  $\forall n \in \text{pre}(c) . \perp \sqsubseteq c(n) \sqsubseteq \top$ .

## Definition (Family of classes $\mathcal{C}$ )

We call the set of all maps from names to bindings the family of classes  $\mathcal{C} := \mathcal{N} \mapsto \mathcal{B}$ .

Several possibilities for composing maps  $\mathcal{C} \square \mathcal{C}$ :

- the symmetric join  $\sqcup$ , defined componentwise:

$$(c_1 \sqcup c_2)(n) = b_1 \sqcup b_2 = \begin{cases} b_2 & \text{if } b_1 = \perp \text{ or } n \notin \text{pre}(c_1) \\ b_1 & \text{if } b_2 = \perp \text{ or } n \notin \text{pre}(c_2) \\ b_2 & \text{if } b_1 = b_2 \\ \top & \text{otherwise} \end{cases} \quad \text{where } b_i = c_i(n)$$

- in contrast, the asymmetric join  $\sqcup\!\!\sqcup$  defined componentwise:

$$(c_1 \sqcup\!\!\sqcup c_2)(n) = \begin{cases} c_1(n) & \text{if } n \in \text{pre}(c_1) \\ c_2(n) & \text{otherwise} \end{cases}$$

## Excursion: Beta-Inheritance

In *Beta*-style inheritance

- the design goal is to provide security wrt. replacement of a method by a different method.
- methods in parents dominate methods in subclass
- the keyword `inner` explicitly delegates control to the subclass

## Definition (Beta inheritance $\triangleleft$ )

Beta inheritance is the binary operator  $\triangleleft : \mathcal{C} \times \mathcal{C} \mapsto \mathcal{C}$ , defined by  $c_1 \triangleleft c_2 = \{\text{inner} \mapsto c_1\} \sqcup\!\!\sqcup (c_2 \sqcup\!\!\sqcup c_1)$

Example (equivalent syntax):

```
class Person {
  String name = "Axel Simon";
  public String toString(){ return name+inner.toString();};
};
class Graduate extends Person {
  public extension String toString(){ return ", Ph.D."; };
};
```

*Smalltalk* inheritance

- children's methods dominate parents' methods
- is the archetype for inheritance in mainstream languages like `Java` or `C#`
- inheriting smalltalk-style establishes a reference to the parent

## Definition (Smalltalk inheritance $\triangleright$ )

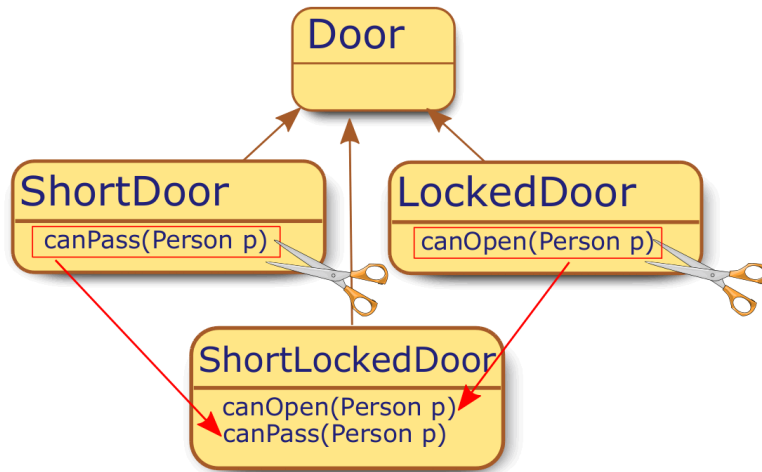
Smalltalk inheritance is the binary operator  $\triangleright : \mathcal{C} \times \mathcal{C} \mapsto \mathcal{C}$ , defined by  $c_1 \triangleright c_2 = \{\text{super} \mapsto c_2\} \sqcup\!\!\sqcup (c_1 \sqcup\!\!\sqcup c_2)$

## Example: Doors

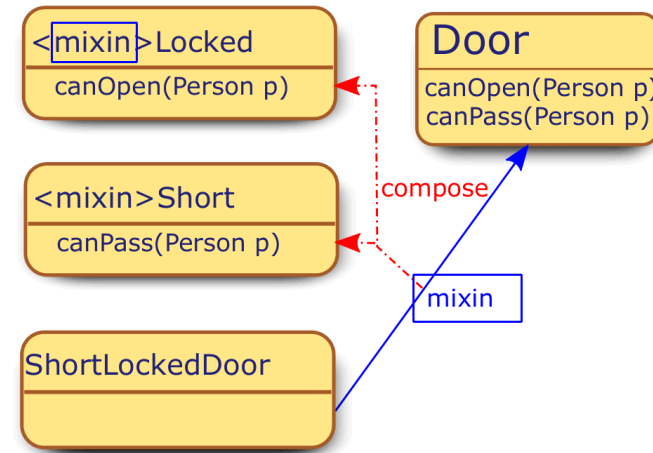
```
Door = {canPass ↦ ⊥, canOpen ↦ ⊥}
LockedDoor = {canOpen ↦ 0x4204711} ⋮ Door
= {super ↦ Door} ⋮ ({canOpen ↦ 0x4204711} ⋮ Door)
= {super ↦ Door, canOpen ↦ 0x4204711, canPass ↦ ⊥}
```

**So what do we really want?**

# Adventure Game with Code Duplication



# Adventure Game with Mixins



# Adventure Game with Mixins



```

class Door {
  boolean canOpen(Person p) { return true; };
  boolean canPass(Person p) { return p.size() < 210; };
}
mixin Locked {
  boolean canOpen(Person p){
    if (!p.hasItem(key)) return false; else return super.canOpen(p);
  }
}
mixin Short {
  boolean canPass(Person p){
    if (p.height()>1) return false; else return super.canPass(p);
  }
}
class ShortDoor = Short(Door);
class LockedDoor = Locked(Door);
mixin ShortLocked = Short o Locked;
class ShortLockedDoor = Short(Locked(Door));
class ShortLockedDoor2 = ShortLocked(Door);
  
```

# Abstract model for Mixins



A Mixin is a *unary second order type expression*. In principle it is a curried version of the Smalltalk-style inheritance operator. In certain languages, programmers can create such mixin operators:

## Definition (Mixin)

The mixin constructor  $mixin : \mathcal{C} \mapsto (\mathcal{C} \mapsto \mathcal{C})$  is a unary class function, creating a unary class operator, defined by:

$$mixin(c) = \lambda x . c \triangleright x$$

**Note:** Mixins can also be composed  $\circ$ :

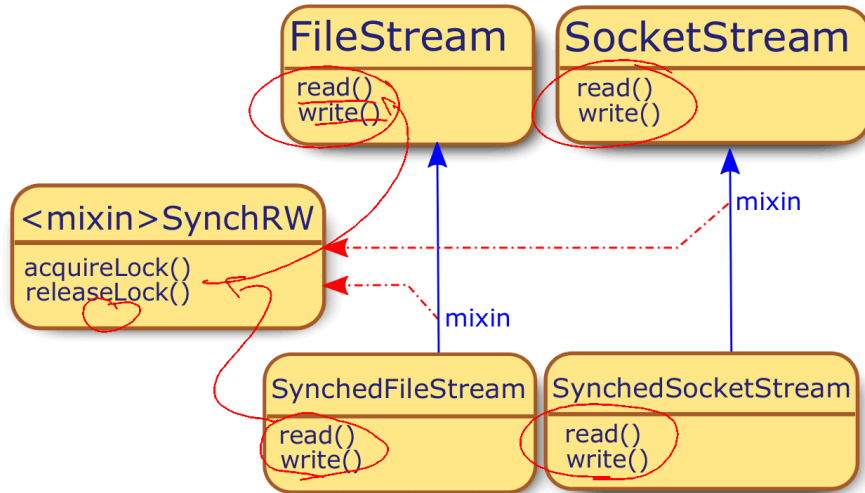
## Example: Doors

$$Locked = \{canOpen \mapsto 0x1234\}$$

$$Short = \{canPass \mapsto 0x4711\}$$

$$Composed = mixin(Short) \circ (mixin(Locked)) = \lambda x . Short \triangleright (Locked \triangleright x) \\ = \lambda x . \{super \mapsto Locked\} \upharpoonright (\{canOpen \mapsto 0x1234, canPass \mapsto 0x4711\} \triangleright x)$$

## Wrapper with Mixins



## Abstract model for Mixins



A Mixin is a *unary second order type expression*. In principle it is a curried version of the Smalltalk-style inheritance operator. In certain languages, programmers can create such mixin operators:

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⚠ Note: Mixins can also be composed  $\circ$ :

### Example: Doors

$$Locked = \{canOpen \mapsto 0x1234\}$$

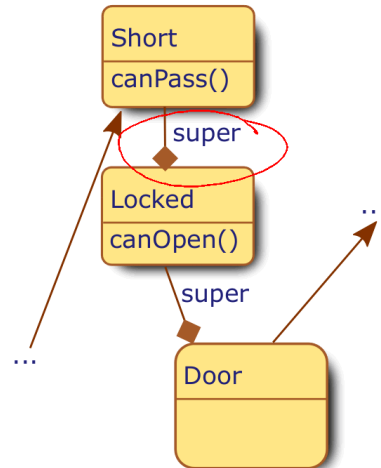
$$Short = \{canPass \mapsto 0x4711\}$$

$$Composed = mixin(Short) \circ (mixin(Locked)) = \lambda x . Short \triangleright (Locked \triangleright x) \\ = \lambda x . \{super \mapsto Locked\} \uplus (\{canOpen \mapsto 0x1234, canPass \mapsto 0x4711\} \triangleright x)$$

## Mixins on Implementation Level



```
class Door {
  boolean canOpen(Person p)...
  boolean canPass(Person p)...
}
mixin Locked {
  boolean canOpen(Person p)...
}
mixin Short {
  boolean canPass(Person p)...
}
class ShortDoor
  = Short(Door);
class ShortLockedDoor
  = Short(Locked(Door));
...
ShortDoor d
  = new ShortLockedDoor();
```



⚠ *non-static* super-References  
 ~> dynamic dispatching without precomputed virtual table

~~Surely multiple inheritance is powerful enough to simulate mixins?~~

C++

## Simulating Mixins in C++



```
template <class Super>
class SyncRW : public Super {
public: virtual int read(){
    acquireLock();
    int result = Super::read();
    releaseLock();
    return result;
};
virtual void write(int n){
    acquireLock();
    Super::write(n);
    releaseLock();
};
// ... acquireLock & releaseLock
};
```

## Simulating Mixins in C++



```
template <class Super>
class SyncRW : public Super {
public: virtual int read(){
    acquireLock();
    int result = Super::read();
    releaseLock();
    return result;
};
virtual void write(int n){
    acquireLock();
    Super::write(n);
    releaseLock();
};
// ... acquireLock & releaseLock
};
```

## Simulating Mixins in C++



```
template <class Super>
class LogOpenClose : public Super {
public: virtual void open(){
    Super::open();
    log("opened");
};
virtual void close(){
    Super::close();
    log("closed");
};
protected: virtual void log(char*s) { ... };
};
class MyDocument : public SyncRW<LogOpenClose<Document>> {};
```

## Simulating Mixins in C++



```
template <class Super>
class LogOpenClose : public Super {
public: virtual void open(){
    Super::open();
    log("opened");
};
virtual void close(){
    Super::close();
    log("closed");
};
protected: virtual void log(char*s) { ... };
};
class MyDocument : public SyncRW<LogOpenClose<Document>> {};
```

## True Mixins vs. C++ Mixins



### True Mixins

- super natively supported
- Mixins as Template do not offer composite mixins
- C++ Type system not modular
- ↪ Mixins have to stay source code
- Hassle-free simple alternative to multiple inheritance

### C++ Mixins

- Mixins reduced to templated superclasses
- Can be seen as coding pattern

### Common properties of Mixins

- Linearization is necessary
- ↪ Exact sequence of Mixins is relevant

## Ruby



```
class Door
  def canOpen (p)
    true
  end
  def canPass(person)
    person.size < 210
  end
end
```

```
module Short
  def canPass(p)
    p.size < 160 and super(p)
  end
end
```

```
module Locked
  def canOpen(p)
    p.hasKey() and super(p)
  end
end
```

```
module ShortLocked
  include Short
  include Locked
end
```

```
class Person
  attr_accessor :size
  def initialize
    @size = 160
  end
  def hasKey
    true
  end
end
```

```
p = Person.new
d = Door.new
d.extend ShortLocked
```

```
puts d.canPass(p)
```

## Ruby



```
class Person
  attr_accessor :size
  def initialize
    @size = 160
  end
  def hasKey
    true
  end
end
```

```
class Door
  def canOpen (p)
    true
  end
  def canPass(person)
    person.size < 210
  end
end
```

```
module Short
  def canPass(p)
    p.size < 160 and super(p)
  end
end
```

```
module Locked
  def canOpen(p)
    p.hasKey() and super(p)
  end
end
```

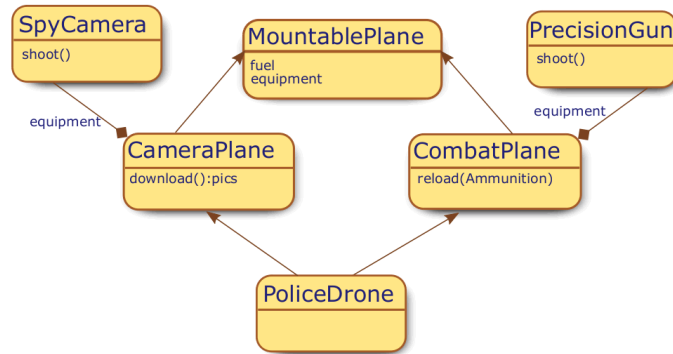
```
class ShortLockedDoor < Door
  include Short
  include Locked
end
```

```
p = Person.new
d = ShortLockedDoor.new
puts d.canPass(p)
```

**Is Inheritance the Ultimate Principle in Reusability?**



## Lack of Control



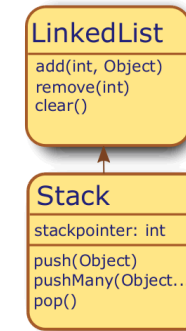
### ⚠ Control

- Common base classes are shared or duplicated at class level

Excerpt from the Java 8 API documentation for class `Properties`:

*“Because `Properties` inherits from `Hashtable`, the `put` and `putAll` methods can be applied to a `Properties` object. Their use is strongly discouraged as they allow the caller to insert entries whose keys or values are not `Strings`. The `setProperty` method should be used instead. If the `store` or `save` method is called on a “compromised” `Properties` object that contains a non-`String` key or value, the call will fail...”*

## Inappropriate Hierarchies



### ⚠ Inappropriate Hierarchies

- High up specified methods *turn obsolete*, but there is no statically safe way to remove them

## The Idea Behind Traits



- A lot of the problems originate from the coupling of implementation and modelling
- Interfaces seem to be hierarchical
- Functionality seems to be modular

### ⚠ Central idea

Separate object *creation* from *modelling hierarchies* and *composing functionality*.

- ↪ Use interfaces to design hierarchical signature propagation
- ↪ Use *traits* as modules for assembling functionality
- ↪ Use classes as frames for entities, which can create objects

# Traits – Composition



## Definition (Trait $\in \mathcal{T}$ )

A class  $t$  is called **trait** iff  $\forall n \in \text{pre}(t) . t(n) \notin \mathbb{N}^+$  (i.e. without attributes)

The **trait sum**  $+$  :  $\mathcal{T} \times \mathcal{T} \mapsto \mathcal{T}$  is the componentwise least upper bound:

$$(c_1 + c_2)(n) = b_1 \sqcup b_2 = \begin{cases} b_2 & \text{if } b_1 = \perp \vee n \notin \text{pre}(c_1) \\ b_1 & \text{if } b_2 = \perp \vee n \notin \text{pre}(c_2) \\ b_2 & \text{if } b_1 = b_2 \\ \top & \text{otherwise} \end{cases} \quad \text{with } b_i = c_i(n)$$

**Trait-Expressions** also comprise:

- **exclusion**  $-$  :  $\mathcal{T} \times \mathcal{N} \mapsto \mathcal{T}$ :  $(t - a)(n) = \begin{cases} \text{undef} & \text{if } a = n \\ t(n) & \text{otherwise} \end{cases}$
- **aliasing**  $[ \rightarrow ]$  :  $\mathcal{T} \times \mathcal{N} \times \mathcal{N} \mapsto \mathcal{T}$ :  $t[a \rightarrow b](n) = \begin{cases} t(n) & \text{if } n \neq a \\ t(b) & \text{if } n = a \end{cases}$

Traits  $t$  can be connected to classes  $c$  by the **asymmetric join**:

$$(c \sqcup t)(n) = \begin{cases} c(n) & \text{if } n \in \text{pre}(c) \\ t(n) & \text{otherwise} \end{cases}$$

Usually, this connection is reserved for the last composition level.

**Can we augment classical languages by traits?**

# Traits – Concepts



## Trait composition principles

- **Flat ordering** All traits have the same precedence under  $+$   
 $\rightsquigarrow$  explicit disambiguation with aliasing and exclusion
- **Precedence** Under asymmetric join  $\sqcup$ , class methods take precedence over trait methods
- **Flattening** After asymmetric join  $\sqcup$ : Non-overridden trait methods have the same semantics as class methods

## ⚠ Conflicts ...

arise if composed traits map methods with identical names to different bodies

## Conflict treatment

- ✓ Methods can be aliased ( $\rightarrow$ )
- ✓ Methods can be excluded ( $-$ )
- ✓ Class methods override trait methods and sort out conflicts ( $\sqcup$ )

# Extension Methods (C#)



## Central Idea:

Uncouple method definitions from class bodies.

Purpose:

- retrospectively add methods to complex types  
 $\rightsquigarrow$  *external definition*
- especially provide definitions of *interface methods*  
 $\rightsquigarrow$  poor man's multiple inheritance!

## Syntax:

- 1 Declare a static class with definitions of static methods
- 2 Explicitly declare first parameter as receiver with modifier `this`
- 3 Import the carrier class into scope (if needed)
- 4 Call extension method in *infix form* with emphasis on the receiver

```

public class Person{
    public int size = 160;
    public bool hasKey() { return true;}
}
public interface Short {}
public interface Locked {}
public static class DoorExtensions {
    public static bool canOpen(this Locked leftHand, Person p){
        return p.hasKey();
    }
    public static bool canPass(this Short leftHand, Person p){
        return p.size<160;
    }
}
public class ShortLockedDoor : Locked,Short {
    public static void Main() {
        ShortLockedDoor d = new ShortLockedDoor();
        Console.WriteLine(d.canOpen(new Person()));
    }
}

```

## Extension Methods as Traits

### Extension Methods

- transparently extend arbitrary types externally
- provide quick relief for plagued programmers

### ...but not traits

- Interface declarations empty, thus kind of purposeless
- Flattening not implemented
- Static scope only

Static scope of extension methods causes unexpected errors:

```

public interface Locked {
    public bool canOpen(Person p);
}
public static class DoorExtensions {
    public static bool canOpen(this Locked leftHand, Person p){
        return p.hasKey();
    }
}

```

## Virtual Extension Methods (Java 8)



Java 8 advances one step further:

```

interface Door {
    boolean canOpen(Person p);
    boolean canPass(Person p);
}
interface Locked {
    default boolean canOpen(Person p) { return p.hasKey(); }
}
interface Short {
    default boolean canPass(Person p) { return p.size<160; }
}
public class ShortLockedDoor implements Short, Locked, Door {
}

```

### Implementation

... consists in adding an interface phase to invoke virtual's name resolution

### Precedence

Still, default methods do not override methods from *abstract classes* when composed

## Traits as General Composition Mechanism



### Central Idea

Separate class generation from hierarchy specification and functional modelling

- 1 model hierarchical relations with interfaces
- 2 compose functionality with traits
- 3 adapt functionality to interfaces and add state via glue code in classes

**Simplified multiple Inheritance without adverse effects**

## Smalltalk

Squeak is a smalltalk implementation, extended with a system for traits.

## Syntax:

- `name: param and: param2`  
declares method name with param1 and param2
- `| ident1 ident2 |`  
declares Variables ident1 and ident2
- `ident := expr`  
assignment
- `object name:content`  
sends message name with content to object ( $\equiv$  call: `object.name(content)`)
- `.`  
line terminator
- `^ expr`  
return statement

## Disambiguation

## Traits vs. Mixins vs. Class-Inheritance

All different kinds of type expressions:

- Definition of curried *second order type operators* + Linearization

*Explicitly:* Traits differ from Mixins

- Traits are applied to a class *in parallel*, Mixins *sequentially*
- Trait *composition is unordered*, avoiding linearization effects
- Traits do *not contain attributes*, avoiding state conflicts
- With traits, *glue code* is concentrated in single classes

```
Trait named: #TRStream uses: TPositionableStream
on: aCollection
  self collection: aCollection.
  self setToStart.
next
  self atEnd
  ifTrue: [nil]
  ifFalse: [self collection at: self nextPosition].
Trait named: #TSynch uses: {}
acquireLock
  self semaphore wait.
releaseLock
  self semaphore signal.

Trait named: #TSyncRStream uses: TSynch+(TRStream(#readNext -> #next))
next
  | read |
  self acquireLock.
  read := self readNext.
  self releaseLock.
  ^ read.
```

## Lessons learned

## Mixins








- Mixins as *low-effort* alternative to multiple inheritance
- Mixins lift type expressions to *second order type expressions*

## Traits

- Implementation Inheritance based approaches leave room for improvement in modularity in real world situations
- Traits offer *fine-grained control* of composition of functionality
- Native trait languages offer *separation of composition* of functionality from *specification* of interfaces

## Further reading...



-  [Gilad Bracha and William Cook.](#)  
**Mixin-based inheritance.**  
*European conference on object-oriented programming on Object-oriented programming systems, languages, and applications (OOPSLA/ECOOP), 1990.*
-  [James Britt.](#)  
**Ruby 2.1.5 core reference, December 2014.**  
URL <https://www.ruby-lang.org/en/documentation/>.
-  [Stéphane Ducasse, Oscar Nierstrasz, Nathanael Schärli, Roel Wuyts, and Andrew P. Black.](#)  
**Traits: A mechanism for fine-grained reuse.**  
*ACM Transactions on Programming Languages and Systems (TOPLAS), 2006.*
-  [Matthew Flatt, Shriram Krishnamurthi, and Matthias Felleisen.](#)  
**Classes and mixins.**  
*Principles of Programming Languages (POPL), 1998.*
-  [Brian Goetz.](#)  
**Interface evolution via virtual extension methods.**  
*JSR 335: Lambda Expressions for the Java Programming Language, 2011.*
-  [Anders Hejlsberg, Scott Wiltamuth, and Peter Golde.](#)  
**C# Language Specification.**  
Addison-Wesley Longman Publishing Co., Inc., Boston, MA, USA, 2003.  
ISBN 0321154916.
-  [Nathanael Schärli, Stéphane Ducasse, Oscar Nierstrasz, and Andrew P. Black.](#)  
**Traits: Composable units of behaviour.**  
*European Conference on Object-Oriented Programming (ECOOP), 2003.*