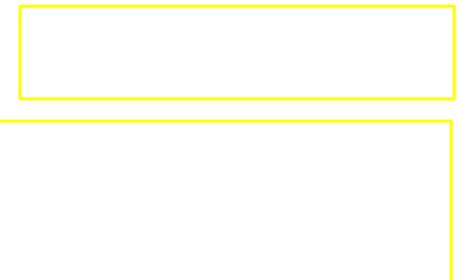


Title: Petter: Programmiersprachen (13.01.2016)
 Date: Wed Jan 13 14:23:23 CET 2016
 Duration: 101:38 min
 Pages: 45

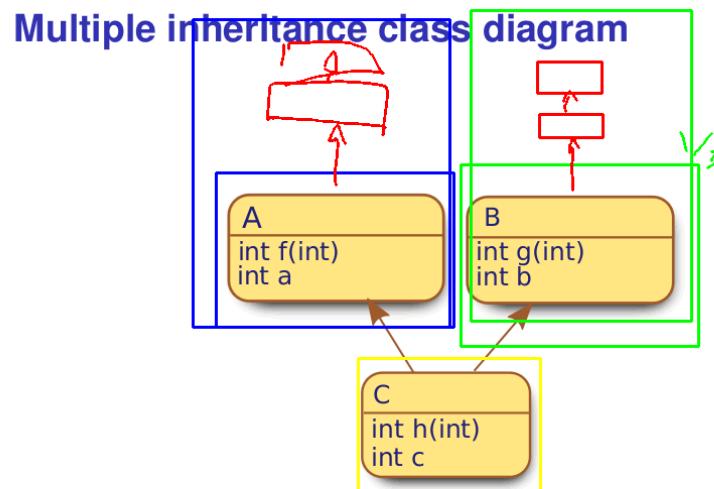
"So how do we include several parent objects?"



Multiple Inheritance

Implementation of Multiple inheritance

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Static Type Casts

```

class A {
    int a; int f(int);
}
class B {
    int b; int g(int);
}
class C : public A, public B {
    int c; int h(int);
}
...
B* b = new C();
  
```

Diagram illustrating static type casting:

A class `C` is shown with three members: `A int a`, `B int b`, and `C int c`. A dashed arrow points from `C` to `A`, and another dashed arrow points from `C` to `B`. To the right, a box labeled $\triangle B$ contains the members `A int a`, `B int b`, and `C int c`. A green arrow points from the `C` member in the `C` class to the `B` member in the $\triangle B$ box.

```

%1 = call i8* @_new(i64 12)
call void @_memset.p0i8.i64(i8* %1, i8 0, i64 12, i32 4, i1 false)
%2 = getelementptr i8* %1, i64 4           ; select B-offset in C
%b = bitcast i8* %2 to %class.B*
  
```



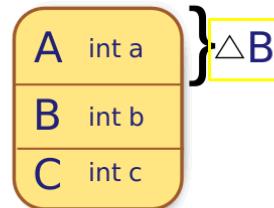
Static Type Casts

```
class A {
    int a; int f(int);
};

class B {
    int b; int g(int);
};

class C : public A , public B {
    int c; int h(int);
};

...
B* b = new C();
```



```
%class.C = type { %class.A, %class.B, i32 }
%class.A = type { i32 }
%class.B = type { i32 }
```

```
%1 = call i8* @_new(i64 12)
call void @_memset.p0i8.i64(i8* %1, i8 0, i64 12, i32 4, i1 false)
%2 = getelementptr i8* %1, i64 4          ; select B-offset in C
%b = bitcast i8* %2 to %class.B*
```

- ⚠ implicit casts potentially add a constant to the object pointer.
- ⚠ getelementptr implements ΔB as $4 \cdot i8!$

Multiple Inheritance

Implementation of Multiple inheritance

Multiple base classes in layout

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Keeping Calling Conventions

```
class A {
    int a; int f(int);
};

class B {
    int b; int g(int);
};

class C : public A , public B {
    int c; int h(int);
};

...
C c;
c.g(42);
```

```
%class.C = type { %class.A, %class.B, i32 }
%class.A = type { i32 }
%class.B = type { i32 }
```

```
%c = alloca %class.C
%1 = bitcast %class.C* %c to i8*
%2 = getelementptr i8* %1, i64 4          ; select B-offset in C
%3 = call i32 @_g(%class.B* %2, i32 42) ; g is statically known
```

Ambiguities

```
class A { void f(int); };
class B { void f(int); };
class C : public A, public B {};
```

```
C* pc;
pc->f(42);
```

- ⚠ Which method is called?

Solution I: Explicit qualification

```
pc->A::f(42);
pc->B::f(42);
```

Solution II: Automagical resolution

Idea: The Compiler introduces a linear order on the nodes of the inheritance graph



Linearization

Principle 1: Inheritance Relation

Defined by parent-child. Example:
 $C(A, B) \Rightarrow C \rightarrow A \wedge C \rightarrow B$

Principle 2: Multiplicity Relation

Defined by the succession of multiple parents. Example:
 $C(A, B) \Rightarrow A \rightarrow B$

In General:

- ➊ Inheritance is a uniform mechanism, and its searches (\rightarrow total order) apply identically for all object fields or methods
- ➋ In the literature, we also find the set of constraints to create a linearization as Method Resolution Order
- ➌ Linearization is a best-effort approach at best

Multiple Inheritance

Implementation of Multiple inheritance

Ambiguities

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Multiple Inheritance

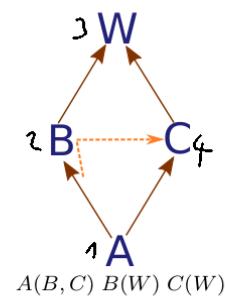
Implementation of Multiple inheritance

Method Resolution Order

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MRO via DFS

Leftmost Preorder Depth-First Search



MRO via DFS

Leftmost Preorder Depth-First Search

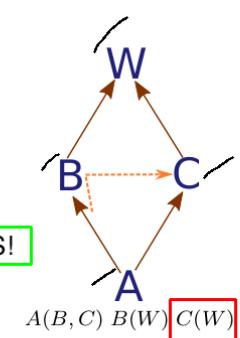
$L[A] = A \boxed{B} W C$

⚠ Principle 1 *inheritance* is violated

Python: classical python objects (≤ 2.1) use LPDFS!

LPDFS with Duplicate Cancellation

$L[A] = A \cancel{B} \cancel{C} W$



MRO via DFS

Leftmost Preorder Depth-First Search

$L[A] = A B W C$

⚠ Principle 1 *inheritance* is violated

Python: classical python objects (≤ 2.1) use LPDFS!

LPDFS with Duplicate Cancellation

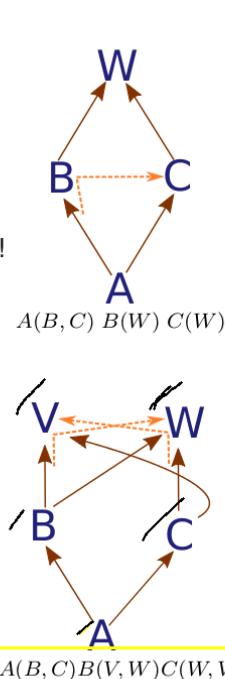
$L[A] = A B C W$

✓ Principle 1 *inheritance* is fixed

Python: new python objects (2.2) use LPDFS(DC)!

LPDFS with Duplicate Cancellation

$A \cancel{B} \cancel{C} W V$



MRO via DFS

Leftmost Preorder Depth-First Search

$L[A] = A B W C$

⚠ Principle 1 *inheritance* is violated

Python: classical python objects (≤ 2.1) use LPDFS!

LPDFS with Duplicate Cancellation

$L[A] = A B C W$

✓ Principle 1 *inheritance* is fixed

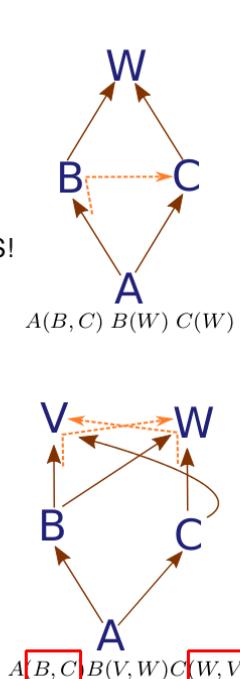
Python: new python objects (2.2) use LPDFS(DC)!

LPDFS with Duplicate Cancellation

$L[A] = A \boxed{B} \boxed{C} W V$

⚠ Principle 2 *multiplicity* not fulfillable

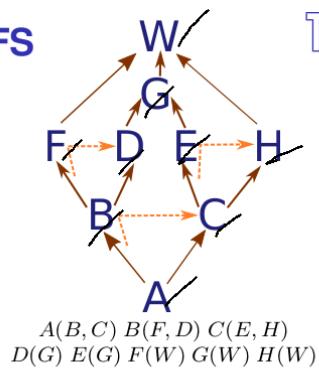
⚠ However $B \rightarrow C \Rightarrow W \rightarrow V??$



MRO via Refined Postorder DFS

Reverse Postorder Rightmost DFS

A B F D C E G H W



$A(B, C)$ $B(F, D)$ $C(E, H)$
 $D(G)$ $E(G)$ $F(W)$ $G(W)$ $H(W)$



MRO via Refined Postorder DFS

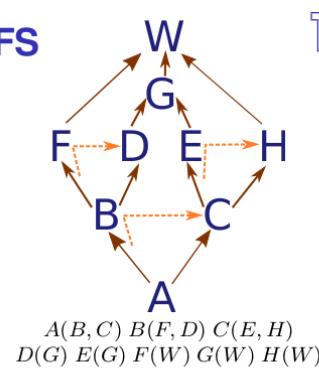
Reverse Postorder Rightmost DFS

$L[A] = A B F D C E G H W$

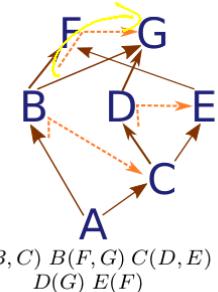
✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS



$A(B, C)$ $B(F, D)$ $C(E, H)$
 $D(G)$ $E(G)$ $F(W)$ $G(W)$ $H(W)$



$A(B, C)$ $B(F, G)$ $C(D, E)$
 $D(G)$ $E(F)$

MRO via Refined Postorder DFS

Reverse Postorder Rightmost DFS

$L[A] = A B F D C E G H W$

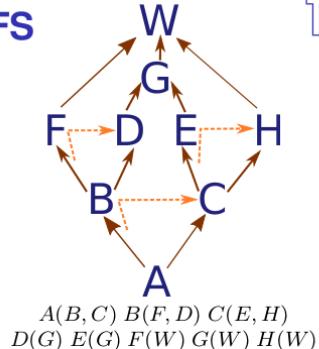
✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS

$L[A] = A B C D G E F$

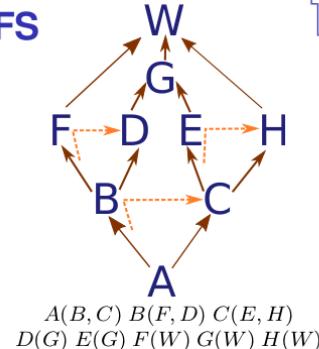
⚠ But principle 2 *multiplicity* is violated!



$A(B, C)$ $B(F, D)$ $C(E, H)$
 $D(G)$ $E(G)$ $F(W)$ $G(W)$ $H(W)$



$A(B, C)$ $B(F, G)$ $C(D, E)$
 $D(G)$ $E(F)$



$A(B, C)$ $B(F, D)$ $C(E, H)$
 $D(G)$ $E(G)$ $F(W)$ $G(W)$ $H(W)$



RPRDFS

$L[A] = A B C D \boxed{G} E F$

⚠ But principle 2 *multiplicity* is violated!

Refined RPRDFS



$A(B, C)$ $B(F, D)$ $C(E, H)$
 $D(G)$ $E(G)$ $F(W)$ $G(W)$ $H(W)$



$A(B, C)$ $B(F, G)$ $C(D, E)$
 $D(G)$ $E(F)$

MRO via Refined Postorder DFS

Reverse Postorder Rightmost DFS

$L[A] = A \ B \ F \ D \ C \ E \ G \ H \ W$

✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS

$L[A] = A \ B \ C \ D \ G \ E \ F$

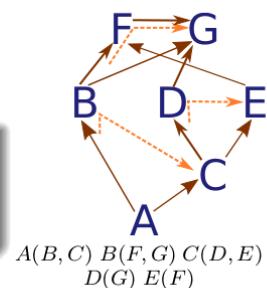
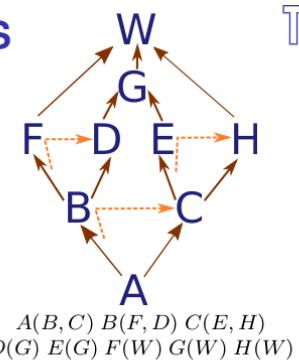
⚠ But principle 2 *multiplicity* is violated!

CLOS uses Refined RPDFS [3]

Refined RPRDFS

$L[A] = A \ B \ C \ D \ E \ F \ G$

✓ Refine graph with conflict edge & rerun RPRDFS!



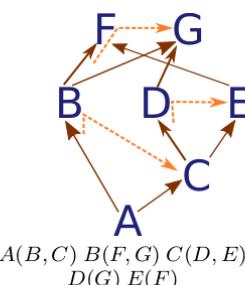
MRO via Refined Postorder DFS

Refined RPRDFS

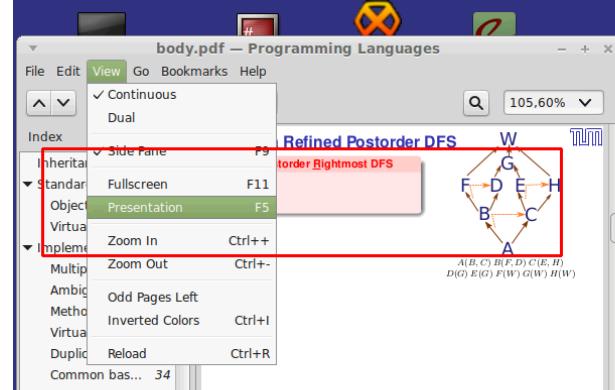
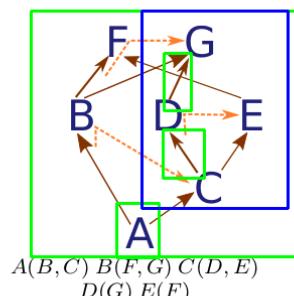
⚠ Monotonicity is not guaranteed!

Extension Principle: Monotonicity

If $C_1 \rightarrow C_2$ in C 's linearization, then $C_1 \rightarrow C_2$ for every linearization of C 's children.



MRO via Refined Postorder DFS



Refined RPRDFS

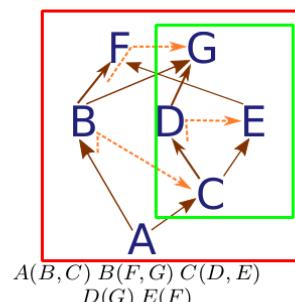
⚠️ Monotonicity is not guaranteed!

Extension Principle: Monotonicity

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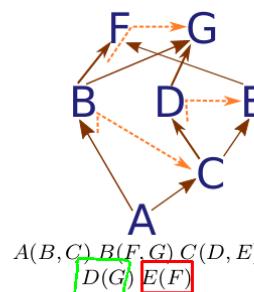
$$L[A] = [A \ B \ C \ D \ E \ F \ G] \implies [F \rightarrow G]$$

$$L[C] = [D \ G \ E \ F] \implies [G \rightarrow F]$$



MRO via C3 Linearization

$$\begin{aligned} L[G] &= G \\ L[F] &= F \\ L[E] &= E \cdot L(F) = EF \\ L[D] &= DG \\ L[B] &= \\ L[C] &= \\ L[A] &= \end{aligned}$$



MRO via C3 Linearization

A linearization L is an attribute $L[C]$ of a class C . Classes B_1, \dots, B_n are superclasses to child class C , defined in the *local precedence order* $C(B_1 \dots B_n)$. Then

$$L[C] = C \cdot \bigsqcup_i (L[B_i], \dots, L[B_n], B_1 \dots B_n) \quad | \quad C(B_1, \dots, B_n)$$

$$L[Object] = Object$$

with

$$\bigsqcup_i (L_i) = \begin{cases} c \cdot (\bigsqcup_i (L_i \setminus c)) & \text{if } \exists_{\min k} \forall_j c = \text{head}(L_k) \notin \text{tail}(L_j) \\ \text{fail} & \text{else} \end{cases}$$

MRO via C3 Linearization

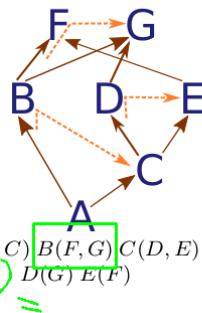
$$\begin{aligned} L[G] &= G \\ L[F] &= F \\ L[E] &= E \cdot F \\ L[D] &= D \cdot G \\ L[B] &= B \cdot \bigsqcup_i (L[F], L[G], F \cdot G) = \\ L[C] &= \\ L[A] &= \end{aligned}$$

$$\begin{aligned} &= B \cdot \bigsqcup_i (F, G, F \cdot G) = \\ &= B \cdot (F \cdot \bigsqcup_i (G, G)) = \\ &= B \cdot F \cdot G \end{aligned}$$

MRO via C3 Linearization



$L[G]$ G
 $L[F]$ F
 $L[E]$ E · F
 $L[D]$ D · G
 $L[B]$ B · (L[F] \sqcup L[E], L[D])
 $L[C]$
 $L[A]$

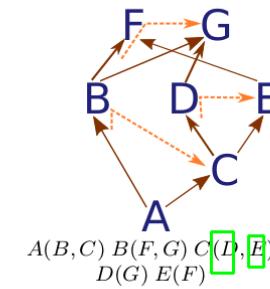


$$\begin{aligned}
 &= B \cdot L(F, G, F \cdot G) - \\
 &= B \cdot (F \cdot L(F, G, G)) = \\
 &= B \cdot F \cdot G
 \end{aligned}$$

MRO via C3 Linearization



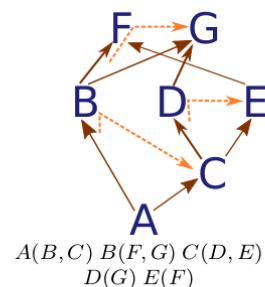
$L[G]$ G
 $L[F]$ F
 $L[E]$ E · F
 $L[D]$ D · G
 $L[B]$ B · F · G
 $L[C]$
 $L[A]$



MRO via C3 Linearization



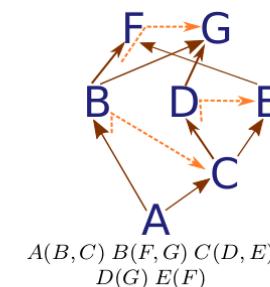
$L[G]$ G
 $L[F]$ F
 $L[E]$ E · F
 $L[D]$ D · G
 $L[B]$ B · F · G
 $L[C]$ C · (L[D] \sqcup L[E] \sqcup (D · E))
 $L[A]$



MRO via C3 Linearization



$L[G]$ G
 $L[F]$ F
 $L[E]$ E · F
 $L[D]$ D · G
 $L[B]$ B · F · G
 $L[C]$ C · ((~~D · E~~) \sqcup (E · F) \sqcup (~~E · D~~))
 $L[A]$



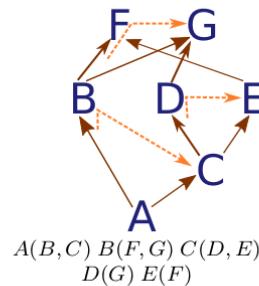
C · D · G · C · F

MRO via C3 Linearization

```

L[G] G
L[F] F
L[E] E · F
L[D] D · G
L[B] B · F · G
L[C] C · D · G · E · F
L[A]

```



Multiple Inheritance

Implementation of Multiple inheritance

Method Resolution Order

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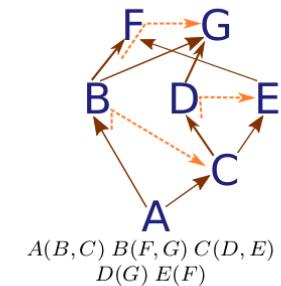


MRO via C3 Linearization

```

L[G] G
L[F] F
L[E] E · F
L[D] D · G
L[B] B · F · G
L[C] C · D · G · E · F
L[A] A · ((B · F · G) ∪ (C · D · G · E · F) ∪ (E · F))
A · B · C · D

```



Multiple Inheritance

Implementation of Multiple inheritance

Method Resolution Order

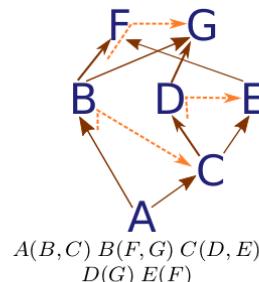
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MRO via C3 Linearization

```

L[G] G
L[F] F
L[E] E · F
L[D] D · G
L[B] B · F · G
L[C] C · D · G · E · F
L[A] ⚠ fail

```



Multiple Inheritance

Implementation of Multiple inheritance

Method Resolution Order

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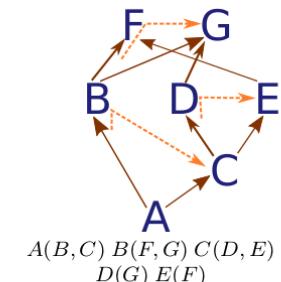


MRO via C3 Linearization

```

L[G] G
L[F] F
L[E] E · F
L[D] D · G
L[B] B · F · G
L[C] C · D · G · E · F
L[A] ⚠ fail

```



C3 detects and reports a violation of *monotonicity* with the addition of $A(B, C)$ to the class set.

C3 linearization [1]: is used in OpenDylan, Python, and Perl 6

Multiple Inheritance

Implementation of Multiple inheritance

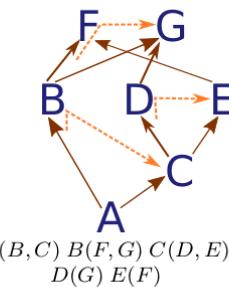
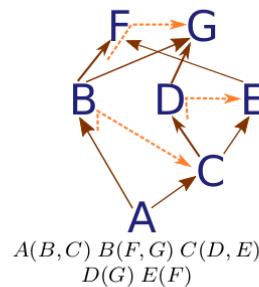
Method Resolution Order

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Method Resolution Order

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$L[G] = G$
 $L[F] = F$
 $L[E] = E \cdot F$
 $L[D] = D \cdot G$
 $L[B] = B \cdot F \cdot G$
 $L[C] = C \cdot D \cdot G \cdot E \cdot F$
 $L[A] = A \cdot B \cdot C \cdot D \cdot ((F \cdot G) \sqcup (G \cdot E \cdot F))$



$L[G] = G$
 $L[F] = F$
 $L[E] = E \cdot F$
 $L[D] = D \cdot G$
 $L[B] = B \cdot F \cdot G$
 $L[C] = C \cdot D \cdot G \cdot E \cdot F$
 $L[A] = A \cdot B \cdot C \cdot D \cdot ((\cancel{F \cdot G}) \sqcup (\cancel{G \cdot E \cdot F}))$

MRO via C3 Linearization

A linearization L is an attribute $L[C]$ of a class C . Classes B_1, \dots, B_n are superclasses to child class C , defined in the *local precedence order* $C(B_1 \dots B_n)$. Then

$$L[C] = C \cdot \bigsqcup(L[B_1], \dots, L[B_n], B_1 \cdot \dots \cdot B_n) \quad | \quad C(B_1, \dots, B_n)$$

$$L[Object] = Object$$

with

$$\bigsqcup_i(L_i) = \begin{cases} c \cdot (\bigsqcup_i(L_i \setminus c)) & \text{if } \exists_{\min k} \forall_j c = head(L_k) \notin tail(L_j) \\ \triangle fail & \text{else} \end{cases}$$

Linearization vs. explicit qualification

Linearization

- No switch/duplexer code necessary
- No explicit naming of qualifiers
- Unique **super reference**
- Reduces number of multi-dispatching conflicts

Qualification

- More flexible, fine-grained
- Linearization choices may be awkward or unexpected

Languages with automatic linearization exist

- **CLOS** Common Lisp Object System
- **Dylan**, **Python** and **Perl 6** with C3
- Prerequisite for → Mixins

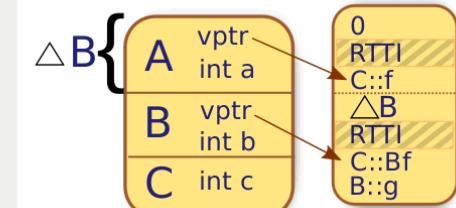
Virtual Tables for Multiple Inheritance

```
class A {
    int a; virtual int f(int);
};

class B {
    int b; virtual int f(int);
    virtual int g(int);
};

class C : public A, public B {
    int c; int f(int);
};

C c;
B* pb = &c;
pb->f(42);
```



```
%class.C = type { %class.A, [12 x i8], i32 }
%class.A = type { i32 (...)**, i32 }
%class.B = type { i32 (...)**, i32 }
```

```
; B* pb = &c;
%0 = bitcast %class.C* %c to i8*           ; type fumbling
%1 = getelementptr i8* %0, i64 16            ; offset of B in C
%2 = bitcast i8* %1 to %class.B*            ; get typing right
store %class.B* %2, %class.B** %pb          ; store to pb
```

Virtual Tables for Multiple Inheritance

```
class A {
    int a; virtual int f(int);
};

class B {
    int b; virtual int f(int);
    virtual int g(int);
};

class C : public A, public B {
    int c; int f(int);
};

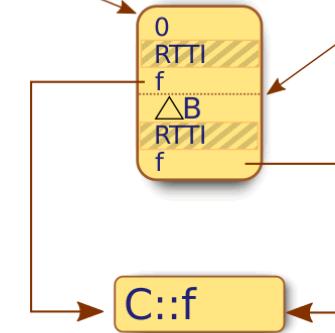
C c;
B* pb = &c;
pb->f(42);

; pb->f(42);
%0 = load %class.B** %pb                   ; load the b-pointer
%1 = bitcast %class.B* %0 to i32 (%class.B*, i32)*** ; cast to vtable
%2 = load i32(%class.B*, i32)*** %1          ; load vptr
%3 = getelementptr i32 (%class.B*, i32)*** %2, i64 0 ; select f() entry
%4 = load i32(%class.B*, i32)*** %3          ; load f()-thunk
%5 = call i32 %(%class.B* %0, i32 42)
```

Casting Issues

```
class A { int a; };
class B { virtual int f(int); };
class C : public A, public B {
    int c; int f(int);
};
C* c = new C();
c->f(42);
```

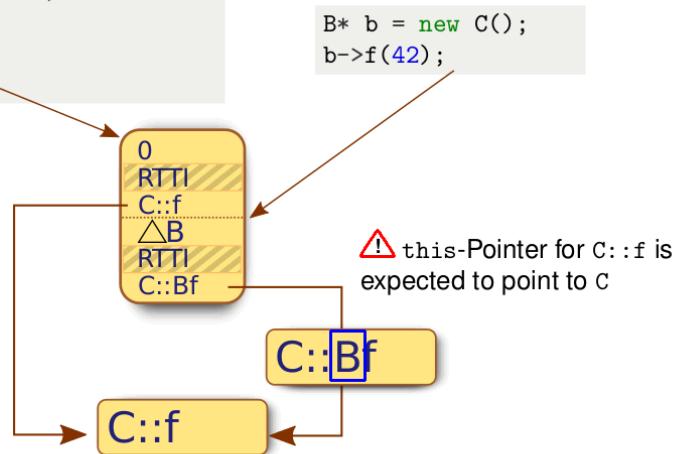
```
B* b = new C();
b->f(42);
```



Casting Issues

```
class A { int a; };
class B { virtual int f(int); };
class C : public A , public B {
    int c; int f(int);
};

C* c = new C();
c->f(42);
```



Thunks

Solution: thunks

...are trampoline methods, delegating the virtual method to its original implementation with an adapted `this`-reference

```
define i32 @_f(%class.B* %this i32 %i) {
    %1 = bitcast %class.B* %this to i8*
    %2 = getelementptr i8* %1, i64 -16           ; sizeof(A)=16
    %3 = bitcast i8* %2 to %class.C*
    %4 = call i32 @_f(%class.C* %3, i32 %i)
    ret i32 %4
}
```

~~> B-in-C-vtable entry for `f(int)` is the thunk `_f(int)`

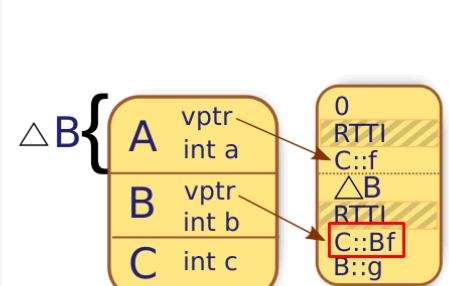
Virtual Tables for Multiple Inheritance

```
class A {
    int a; virtual int f(int);
};

class B {
    int b; virtual int f(int);
    virtual int g(int);
};

class C : public A , public B {
    int c; int f(int);
};

C c;
B* pb = &c;
pb->f(42);
```



```
%class.C = type { %class.A, [12 x i8], i32 }
%class.A = type { i32 (...)**, i32 }
%class.B = type { i32 (...)**, i32 }
```

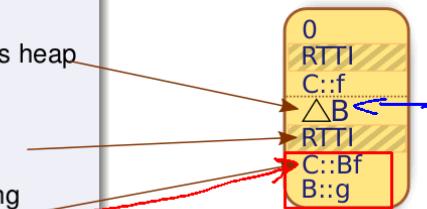
```
; pb->f(42);
%0 = load %class.B** %pb                ; load the b-pointer
%1 = bitcast %class.B* %0 to i32 (%class.B*, i32)*** ; cast to vtable
%2 = load i32(%class.B*, i32)*** %1          ; load vptr
%3 = getelementptr i32 (%class.B*, i32)** %2, i64 0 ; select f() entry
%4 = load i32(%class.B*, i32)** %3          ; load f()-thunk
%5 = call i32 %4(%class.B* %0, i32 42)
```

Basic Virtual Tables (~ C++-ABI)

A Basic Virtual Table

consists of different parts:

- ① *offset to top* of an enclosing objects heap representation
- ② *typeinfo pointer* to an RTTI object (not relevant for us)
- ③ *virtual function pointers* for resolving virtual methods



- Virtual tables are composed when multiple inheritance is used
- The `vptr` fields in objects are pointers to their corresponding virtual-subtables
- Casting preserves the link between an object and its corresponding virtual-table
- `clang -cc1 -fdump-vtable-layouts -emit-llvm code.cpp` yields the vtables of a compilation unit

Virtual Tables for Multiple Inheritance

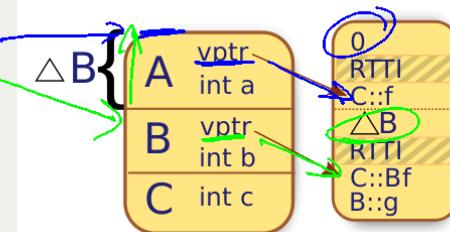
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%2 = load i32(%class.B*, i32)*** %1           ;load vptr
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