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Programming Languages

Multiple Inheritance

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Winter term 2014

Multiple Inheritance

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Outline



Inheritance Principles

- ① Interface Inheritance
- ② Implementation Inheritance
- ③ Liskov Substitution Principle and Shapes

C++ Object Heap Layout

- ① Basics
- ② Single-Inheritance
- ③ Virtual Methods

C++ Multiple Parents Heap Layout

- ① Multiple-Inheritance
- ② Virtual Methods
- ③ Common Parents

Discussion & Learning Outcomes

Multiple Inheritance

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Outline



Inheritance Principles

- ① Interface Inheritance
- ② Implementation Inheritance
- ③ Liskov Substitution Principle and Shapes

C++ Object Heap Layout

- ① Basics
- ② Single-Inheritance
- ③ Virtual Methods

Excuse: Linearization

- ① Ambiguous common parents
- ② Principles of Linearization
- ③ Linearization algorithms

C++ Multiple Parents Heap Layout

- ① Multiple-Inheritance
- ② Virtual Methods
- ③ Common Parents

Discussion & Learning Outcomes

Multiple Inheritance

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Interface vs. Implementation inheritance

"Wouldn't it be nice to inherit from several parents?"

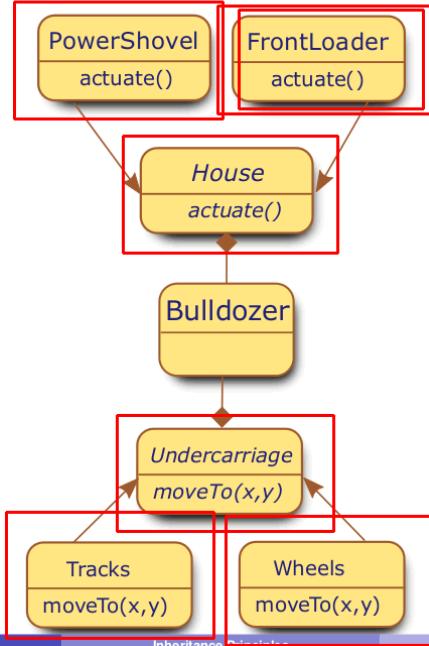
The classic motivation for inheritance is implementation inheritance

- *Code reuse*
- Child specializes parents, replacing particular methods with custom ones
- Parent acts as library of common behaviours
- Implemented in languages like C++ or Lisp

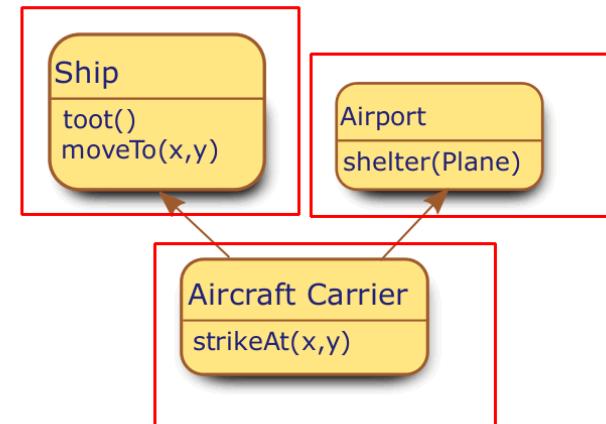
Code sharing in interface inheritance inverts this relation

- *Behaviour contract*
- Child provides methods, with signatures predetermined by the parent
- Parent acts as generic code frame with room for customization
- Implemented in languages like Java or C#

Interface Inheritance



Implementation inheritance



Excursion: LSP and Square-Rect-Problem



The Liskov Substitution Principle

Functions that use pointers or references to base classes must be able to use objects of derived classes without knowing it.

```
class Rectangle {  
    void setWidth (int w){ this.w=w; }  
    void setHeight(int h){ this.h=h; }  
    void getWidth () { return w; }  
    void getHeight() { return h; }  
}  
  
class Square extends Rectangle {  
    void setWidth (int w){ this.w=w;h=w; }  
    void setHeight(int h){ this.h=h;w=h; }  
}
```

```
Rectangle r =  
    new Square(2);  
r.setWidth(3);  
r.setHeight(4);  
assert r.getHeight()*  
    r.getWidth()==12;
```

Excursion: LSP and Square-Rect-Problem



The Liskov Substitution Principle

Functions that use pointers or references to base classes must be able to use objects of derived classes without knowing it.

```
class Rectangle {  
    void setWidth (int w){ this.w=w; }  
    void setHeight(int h){ this.h=h; }  
    void getWidth () { return w; }  
    void getHeight() { return h; }  
}  
  
class Square extends Rectangle {  
    void setWidth (int w){ this.w=w;h=w; }  
    void setHeight(int h){ this.h=h;w=h; }  
}
```

```
Rectangle r =  
    new Square(2);  
r.setWidth(3);  
r.setHeight(4);  
assert r.getHeight()*  
    r.getWidth()==12;
```

⚠ Behavioural assumptions

"So how do we lay out objects in heap anyway?"

Excursion: Brief introduction to LLVM IR



Low Level Virtual Machine as reference semantics:

```
; (recursive) struct definitions  
%struct.A = type { i32, %struct.B, i32(i32)* }  
%struct.B = type { i64, [10 x [20 x i32]], i8 }
```

; allocation of objects

```
%a = alloca %struct.A  
; address computation for selection in structure (pointers):  
%1 = getelementptr %struct.A* %a, i64 0, i64 2  
; load from memory  
%2 = load i32(i32)* %1  
; indirect call  
%retval = call i32 (i32)* %2(i32 42)
```

Retrieve the memory layout of a compilation unit with:

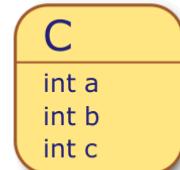
```
clang -cc1 -x c++ -v -fdump-record-layouts -emit-llvm source.cpp
```

Retrieve the IR Code of a compilation unit with:

```
clang -O1 -S -emit-llvm source.cpp -o IR.llvm
```

Object layout

```
class A {  
    int a; int f(int);  
};  
class B : public A {  
    int b; int g(int);  
};  
class C : public B {  
    int c; int h(int);  
};  
  
...  
  
C c;  
c.g(42);
```

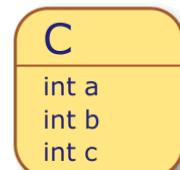


```
%class.C = type { %class.B, i32 }  
%class.B = type { %class.A, i32 }  
%class.A = type { i32 }
```

```
%c = alloca %class.C  
%1 = bitcast %class.C* %c to %class.B*  
%2 = call i32 @_g(%class.B* %1, i32 42) ; g is statically known
```

Object layout

```
class A {  
    int a; int f(int);  
};  
class B : public A {  
    int b; int g(int);  
};  
class C : public B {  
    int c; int h(int);  
};  
  
...  
  
C c;  
c.g(42);
```

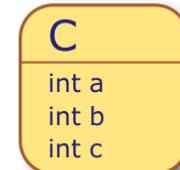


```
%class.C = type { %class.B, i32 }  
%class.B = type { %class.A, i32 }  
%class.A = type { i32 }
```

```
%c = alloca %class.C  
%1 = bitcast %class.C* %c to %class.B*  
%2 = call i32 @_g(%class.B* %1, i32 42) ; g is statically known
```

Translation of a method body

```
class A {  
    int a; int f(int);  
};  
class B : public A {  
    int b; int g(int);  
};  
class C : public B {  
    int c; int h(int);  
};  
  
int B::g(int p) {  
    return p+b;  
};
```

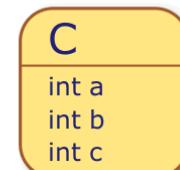


```
%class.C = type { %class.B, i32 }  
%class.B = type { %class.A, i32 }  
%class.A = type { i32 }
```

```
define i32 @_g(%class.B* %this, i32 %p) {  
%1 = getelementptr %class.B* %this, i64 0, i32 1  
%2 = load i32* %1  
%3 = add i32 %2, %p  
ret i32 %3  
}
```

Translation of a method body

```
class A {  
    int a; int f(int);  
};  
class B : public A {  
    int b; int g(int);  
};  
class C : public B {  
    int c; int h(int);  
};  
  
int B::g(int p) {  
    return p+b;  
};
```



```
%class.C = type { %class.B, i32 }  
%class.B = type { %class.A, i32 }  
%class.A = type { i32 }
```

```
define i32 @_g(%class.B* %this, i32 %p) {  
%1 = getelementptr %class.B* %this, i64 0, i32 1  
%2 = load i32* %1  
%3 = add i32 %2, %p  
ret i32 %3  
}
```

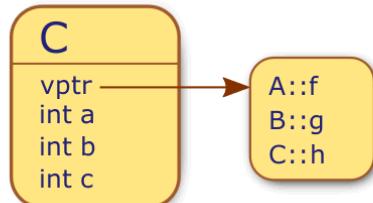
Object layout – virtual methods

```
class A {
    int a; virtual int f(int);
    virtual int g(int);
    virtual int h(int);
};

class B : public A {
    int b; int g(int);
};

class C : public B {
    int c; int h(int);
};

...
C c;
c.g(42);
```

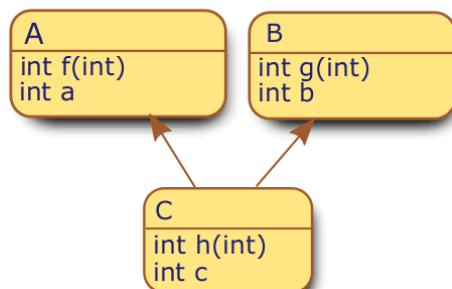


```
%class.C = type { %class.B, i32, [4 x i8] }
%class.B = type { [12 x i8], i32 }
%class.A = type { i32 (...)**, i32 }
```

```
%c.vptr = bitcast %class.C* %c to i32 (%class.B*, i32)*** ; vtbl
%1 = load (%class.B*, i32)*** %c.vptr      ; dereference vptr
%2 = getelementptr %1, i64 1                ; select g()-entry
%3 = load (%class.B*, i32)** %2             ; dereference g()-entry
%4 = call i32 %3(%class.B* %c, i32 42)
```

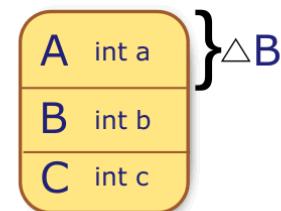
“So how do we include several parent objects?”

Multiple inheritance class diagram



Multiple Base Classes

```
class A {
    int a; int f(int);
};
class B {
    int b; int g(int);
};
class C : public A , public B {
    int c; int h(int);
};
...
C c;
c.g(42);
```

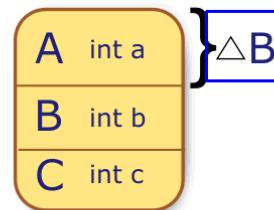


```
%class.C = type { %class.A, %class.B, i32 }
%class.A = type { i32 }
%class.B = type { i32 }
```

```
%c = alloca %class.C
%1 = bitcast %class.C* %c to i8*
%2 = getelementptr i8* %1, i64 4           ; select B-offset in C
%3 = call i32 @_g(%class.B* %2, i32 42)   ; g is statically known
```

Multiple Base Classes

```
class A {  
    int a; int f(int);  
};  
class B {  
    int b; int g(int);  
};  
class C : public A , public B {  
    int c; int h(int);  
};  
...  
C c;  
c.g(42);
```



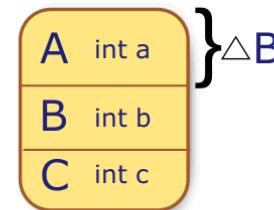
```
%class.C = type { %class.A, %class.B, i32 }  
%class.A = type { i32 }  
%class.B = type { i32 }
```

```
%c = alloca %class.C  
%1 = bitcast %class.C* %c to i8*  
%2 = getelementptr i8* %1, i64 4          ; select B-offset in C  
%3 = call i32 @_g(%class.B* %2, i32 42) ; g is statically known
```

⚠ getelementptr implements ΔB as $4 \cdot i8!$

Static Type Casts

```
class A {  
    int a; int f(int);  
};  
class B {  
    int b; int g(int);  
};  
class C : public A , public B {  
    int c; int h(int);  
};  
...  
B* b = new C();
```



```
%class.C = type { %class.A, %class.B, i32 }  
%class.A = type { i32 }  
%class.B = type { i32 }
```

```
%1 = call i8* @_new(i64 12)  
call void @_memset.p0i8.i64(i8* %1, i8 0, i64 12, i32 4, i1 false)  
%2 = getelementptr i8* %1, i64 4  
%b = bitcast i8* %2 to %class.B*
```

Ambiguities

```
class A { void f(int); };  
class B { void f(int); };  
class C : public A, public B {};
```

```
C* pc;  
pc->f(42)
```

⚠ Which method is called?

Solution I: Explicit qualification

```
pc->A::f(42);  
pc->B::f(42);
```

Solution II: Automagical resolution

Idea: The Compiler introduces a linear order on the nodes of the inheritance graph

Linearization

Principle 1: Inheritance Relation

Defined by parent-child. Example:

$C(A, B) \Rightarrow C \rightarrow A \wedge C \rightarrow B$

Principle 2: Multiplicity Relation

Defined by the succession of multiple parents. Example:

$C(A, B) \Rightarrow A \rightarrow B$

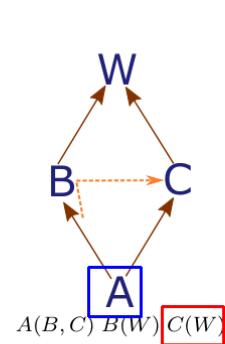
In General:

- ① Inheritance is a uniform mechanism, and its searches (\rightarrow total order) apply identically for all object fields or methods
- ② In the literature, we also find the set of constraints to create a linearization as Method Resolution Order
- ③ Linearization is a best-effort approach at best

MRO via DFS

Leftmost Preorder Depth-First Search

A B WC



Multiple Inheritance

Implementation of Multiple inheritance

Method Resolution Order

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MRO via DFS

Leftmost Preorder Depth-First Search

$L[A] = A \ B \ W \ C$

⚠ Principle 1 *inheritance* is violated

Python: classical python objects (≤ 2.1) use LPDFS!

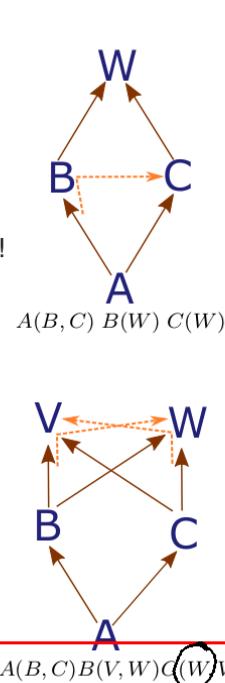
LPDFS with Duplicate Cancellation

$L[A] = A \ B \ C \ W$

✓ Principle 1 *inheritance* is fixed

LPDFS with Duplicate Cancellation

A B WC W V



Method Resolution Order

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MRO via DFS

Leftmost Preorder Depth-First Search

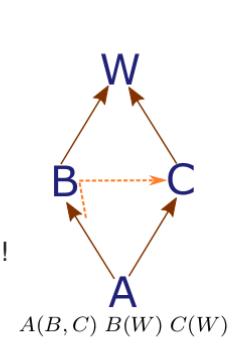
$L[A] = A \ B \ W \ C$

⚠ Principle 1 *inheritance* is violated

Python: classical python objects (≤ 2.1) use LPDFS!

LPDFS with Duplicate Cancellation

A B WC W



Multiple Inheritance

Implementation of Multiple inheritance

Method Resolution Order

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MRO via DFS

Leftmost Preorder Depth-First Search

$L[A] = A \ B \ W \ C$

⚠ Principle 1 *inheritance* is violated

Python: classical python objects (≤ 2.1) use LPDFS!

LPDFS with Duplicate Cancellation

$L[A] = A \ B \ C \ W$

✓ Principle 1 *inheritance* is fixed

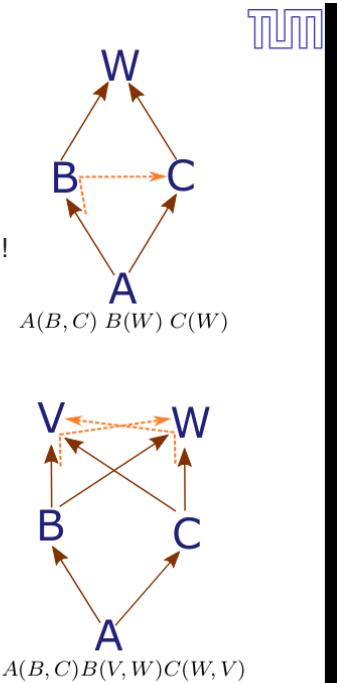
Python: new python objects (2.2) use LPDFS(DC)!

LPDFS with Duplicate Cancellation

$L[A] = A \ B \ C \ W \ V$

⚠ Principle 2 *multiplicity* not fulfillable

⚠ However $B \rightarrow C \Rightarrow W \rightarrow V??$



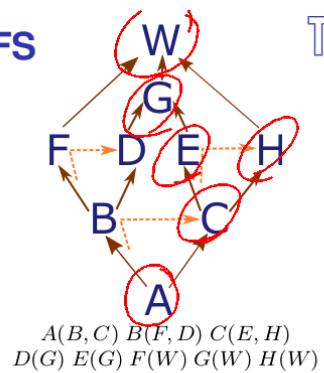
Method Resolution Order

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MRO via Refined Postorder DFS

Reverse Postorder Rightmost DFS

E G H W



MRO via Refined Postorder DFS

Reverse Postorder Rightmost DFS

$L[A] = A B F D C E G H W$

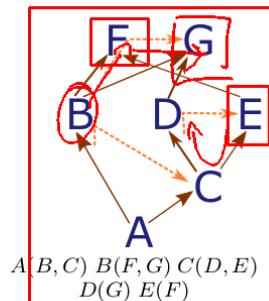
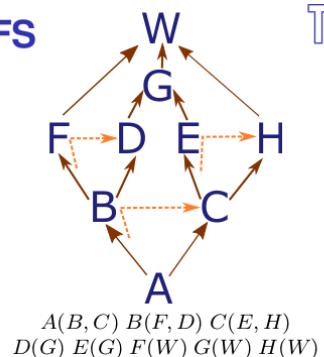
✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS

$L[A] = A B C D G E F$

⚠ But principle 2 *multiplicity* is violated!



MRO via Refined Postorder DFS

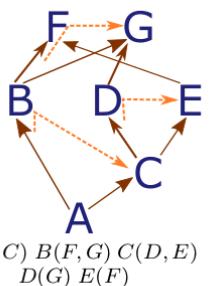
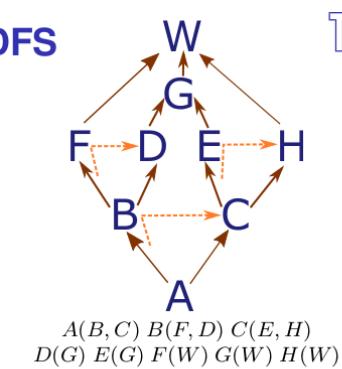
Reverse Postorder Rightmost DFS

$L[A] = A B F D C E G H W$

✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS



MRO via Refined Postorder DFS

Reverse Postorder Rightmost DFS

$L[A] = A B F D C E G H W$

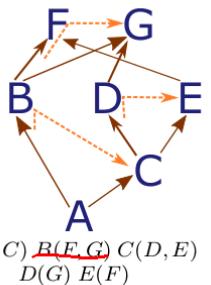
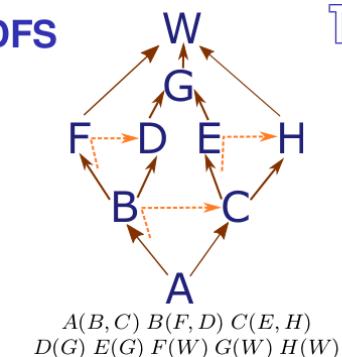
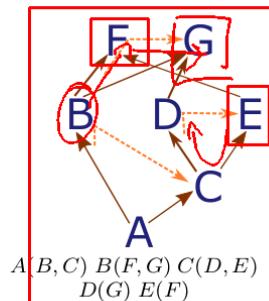
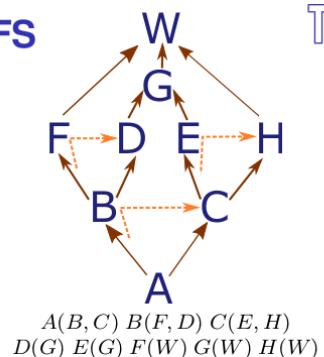
✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS

$L[A] = A B C D G E F$

⚠ But principle 2 *multiplicity* is violated!



MRO via Refined Postorder DFS



Reverse Postorder Rightmost DFS

$L[A] = A \ B \ F \ D \ C \ E \ G \ H \ W$

✓ Linear extension of inheritance relation

↝ Topological sorting

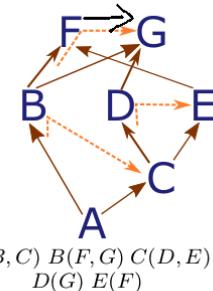
RPRDFS

$L[A] = A \ B \ C \ D \ G \ E \ F$

⚠ But principle 2 *multiplicity* is violated!

Refined RPRDFS

$A(B, C) \ B(F, D) \ C(E, H)$
 $D(G) \ E(G) \ F(W) \ G(W) \ H(W)$



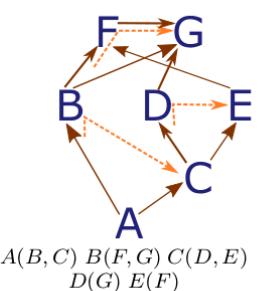
Multiple Inheritance

Implementation of Multiple inheritance

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$A(B, C) \ B(F, D) \ C(E, H)$
 $D(G) \ E(G) \ F(W) \ G(W) \ H(W)$



Multiple Inheritance

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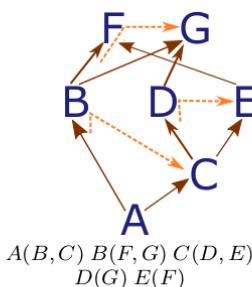
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MRO via Refined Postorder DFS



Extension Principle: Monotonicity

If $C_1 \rightarrow C_2$ in C 's linearization, then $C_1 \rightarrow C_2$ for every linearization of C 's children.



$A(B, C) \ B(F, G) \ C(D, E)$
 $D(G) \ E(F)$

Multiple Inheritance

Implementation of Multiple inheritance

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MRO via Refined Postorder DFS



Reverse Postorder Rightmost DFS

$L[A] = A \ B \ F \ D \ C \ E \ G \ H \ W$

✓ Linear extension of inheritance relation

↝ Topological sorting

RPRDFS

$L[A] = A \ B \ C \ D \ G \ E \ F$

⚠ But principle 2 *multiplicity* is violated!

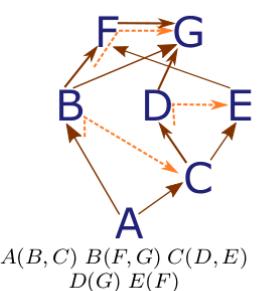
CLOS: uses Refined RPDFS [3]

Refined RPRDFS

$L[A] = A \ B \ C \ D \ E \ F \ G$

✓ Refine graph with conflict edge & rerun RPRDFS!

$A(B, C) \ B(F, D) \ C(E, H)$
 $D(G) \ E(G) \ F(W) \ G(W) \ H(W)$



Multiple Inheritance

Implementation of Multiple inheritance

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MRO via Refined Postorder DFS



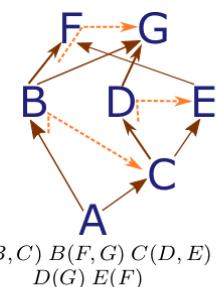
Refined RPRDFS

⚠ *Monotonicity* is not guaranteed!

Extension Principle: Monotonicity

Extension Principle: Monotonicity

If $C_1 \rightarrow C_2$ in C 's linearization, then $C_1 \rightarrow C_2$ for every linearization of C 's children.



$A(B, C) \ B(F, G) \ C(D, E)$
 $D(G) \ E(F)$

Multiple Inheritance

Implementation of Multiple inheritance

Method Resolution Order

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MRO via Refined Postorder DFS

Refined RPRDFS

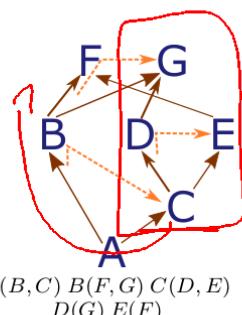
⚠️ Monotonicity is not guaranteed!

Extension Principle: Monotonicity

If $C_1 \rightarrow C_2$ in C 's linearization, then $C_1 \rightarrow C_2$ for every linearization of C 's children.

$$L[A] = A \ B \ C \ D \ E \ F \ G \implies F \rightarrow G$$

$$L[C] = \boxed{D \ G \ E \ F} \implies G \rightarrow F$$



MRO via C3 Linearization



A linearization L is an attribute $L[C]$ of a class C . Classes $B_1 \dots B_n$ are superclasses to child class C , defined in the *local precedence order* $C(B_1 \dots B_n)$. Then

$$L[C(B_1 \dots B_n)] = C \cdot \bigsqcup(L[B_1] \dots L[B_n], B_1 \dots B_n)$$

$$L[Object] = Object$$

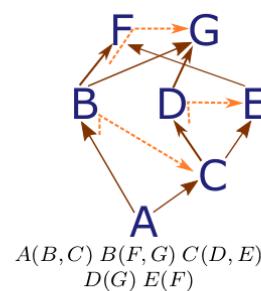
with

$$\bigsqcup(L_i) = \begin{cases} c \cdot (tail(L_k) \sqcup \bigsqcup_{j \neq k} (L_j \setminus c)) & \text{if } \exists_{\min k} c = head(L_k) \notin tail(L_j) \\ \text{! fail} & \text{else} \end{cases}$$



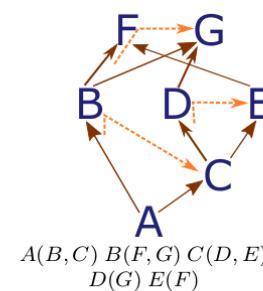
MRO via C3 Linearization

$$\begin{aligned} L[G] &= G \\ L[F] &= F \\ L[E(F)] &= \\ L[D(G)] &= \\ L[B(F, G)] &= \\ L[C(D, E)] &= \\ L[A(B, C)] &= \end{aligned}$$



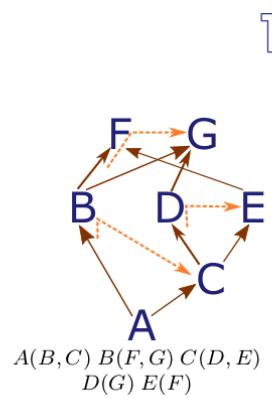
MRO via C3 Linearization

$$\begin{aligned} L[G] &= G \\ L[F] &= F \\ L[E(F)] &= E \ F \\ L[D(G)] &= D \ G \\ L[B(F, G)] &= \\ L[C(D, E)] &= \\ L[A(B, C)] &= \end{aligned}$$



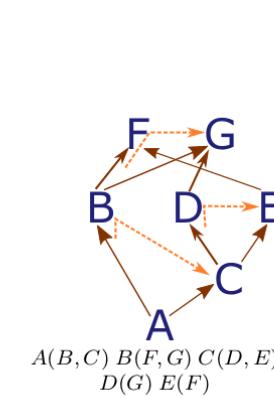
MRO via C3 Linearization

$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B \cdot (L[F] \sqcup L[G] \sqcup \{F, G\})$
$L[C(D,E)]$	
$L[A(B,C)]$	



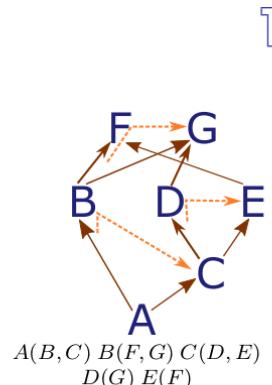
MRO via C3 Linearization

$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B \cdot (\{F\} \sqcup \{G\} \sqcup \{F, G\})$
$L[C(D,E)]$	
$L[A(B,C)]$	



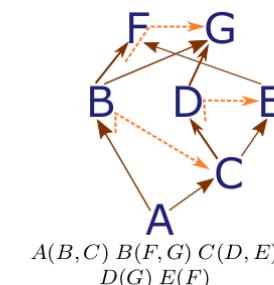
MRO via C3 Linearization

$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B F G$
$L[C(D,E)]$	$C \cdot (\{D, G\} \sqcup \{E, F\} \sqcup \{D, E\})$
$L[A(B,C)]$	



MRO via C3 Linearization

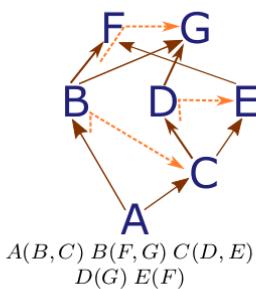
$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B F G$
$L[C(D,E)]$	$C \cdot D \cdot (\{G\} \sqcup \{E, F\} \sqcup \{E\})$
$L[A(B,C)]$	



MRO via C3 Linearization



$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B F G$
$L[C(D,E)]$	$C D G E F$
$L[A(B,C)]$	$A \cdot (\{B,F,G\} \sqcup \{C,D,G,E,F\} \sqcup \{B,C\})$



MRO via C3 Linearization

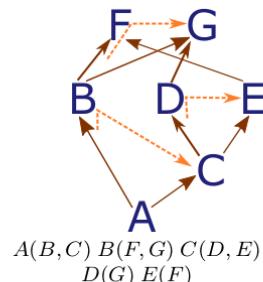


$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B F G$
$L[C(D,E)]$	$C D G E F$
$L[A(B,C)]$	$A \cdot B \cdot C \cdot D \cdot (\{F,G\} \sqcup \{G,E,F\})$

MRO via C3 Linearization



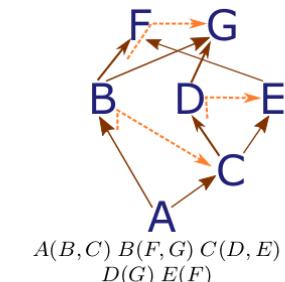
$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B F G$
$L[C(D,E)]$	$C D G E F$
$L[A(B,C)]$	⚠ fail



MRO via C3 Linearization



$L[G]$	G
$L[F]$	F
$L[E(F)]$	$E F$
$L[D(G)]$	$D G$
$L[B(F,G)]$	$B F G$
$L[C(D,E)]$	$C D G E F$
$L[A(B,C)]$	⚠ fail



C3 detects and reports a violation of *monotonicity* with the addition of $A(B,C)$ to the class set.

C3 linearization [1]: is used in OpenDylan, Python, and Perl 6

Linearization

- No switch/duplexer code necessary
- No explicit naming of qualifiers
- Unique super reference
- Reduces number of multi-dispatching conflicts

Qualification

- More flexible, fine-grained
- Linearization choices may be awkward or unexpected

Languages with automatic linearization exist

- *CLOS* Common Lisp Object System
- *Dylan*, *Python* and *Perl 6* with C3
- Prerequisite for → Mixins

“And what about dynamic dispatching in Multiple Inheritance?”