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**Compiler Construction I** 

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SoSe 2014

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Title: Simon: Compilerbau (30.06.2014)

Date: Mon Jun 30 14:15:39 CEST 2014

Duration: 90:40 min

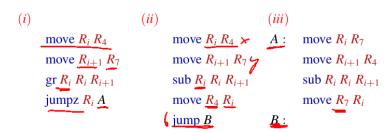
Pages: 58

## **Example for if-statement**

codi; ep aodi, ep

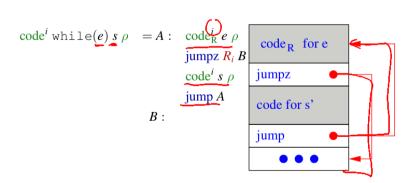
Let  $\rho = \{x \mapsto 4, y \mapsto 7\}$  and let s be the statement

Then  $code^i s \rho$  yields:



# **Iterating Statements**

We only consider the loop  $s \equiv \mathbf{while}\;(e)\;s'.$  For this statement we define:



## **Example: Translation of Loops**

Let  $\rho = \{a \mapsto 7, b \mapsto 8, c \mapsto 9\}$  and let *s* be the statement:

while 
$$(a>0)$$
 {  $/*(i)*/$   
 $c = c + 1;$   $/*(ii)*/$   
 $a = a - b;$   $/*(iii)*/$   
}

Then  $code^{i}$  s  $\rho$  evaluates to:

A: move Ri Rq

kode Ritt O

gr Ri Ri Ritt

jumpe Ri B

move Ri Rg

kode Ritt 7

add Ri Ri Ritt

move Rg Ri

B:

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## **Example: Translation of Loops**

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Then  $code^i s \rho$  evaluates to:

(i) (ii) (iii) (iii)

$$A: \text{ move } R_i R_7 \text{ move } R_i R_9 \text{ move } R_i R_7 \text{ loadc } R_{i+1} 0 \text{ loadc } R_{i+1} 1 \text{ move } R_{i+1} R_8 \text{ sub } R_i R_{i+1} \text{ jumpz } R_i B \text{ move } R_9 R_i \text{ move } R_7 R_i \text{ jump } A$$
 $B:$ 

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## for-Loops

The **for**-loop  $s \equiv$  **for**  $(e_1, e_2, e_3)$  s' is equivalent to the statement sequence  $e_1$ ; while  $(e_2)$   $\{s' e_3\}$  - as long as s' does not contain a continue statement.

Thus, we translate:

$$\operatorname{code}^{i}\operatorname{for}(e_{1};e_{2};e_{3})\ s\ 
ho = \operatorname{code}_{R}^{i}\ e_{1}\ 
ho$$

$$A: \operatorname{code}_{R}^{i}\ e_{2}\ 
ho$$

$$\operatorname{jumpz}\ R_{i}\ B$$

$$\operatorname{code}^{i}\ s\ 
ho$$

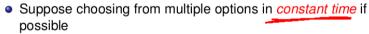
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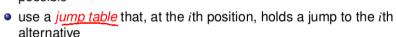
$$\operatorname{jump}\ A$$

$$B:$$

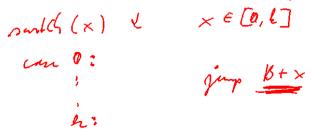
## The switch-Statement

Idea:





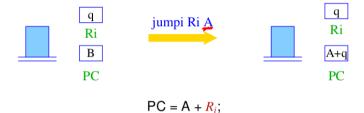
• in order to realize this idea, we need an *indirect jump* instruction



#### The switch-Statement

#### Idea:

- Suppose choosing from multiple options in constant time if possible
- use a *jump table* that, at the *i*th position, holds a jump to the *i*th alternative
- in order to realize this idea, we need an indirect jump instruction



#### **Consecutive Alternatives**

```
Let switch s be given with k consecutive case alternatives: switch (e) {
    case c_0: s_0; break;
    :
    case c_{k-1}: s_{k-1}; break;
    default: s; break;
}
that is, c_i + 1 = c_{i+1} for i = [0, k-1].
```

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```
switch (e) {
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    \( \text{is} \)
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    default: s_i^* break;
}

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Define \operatorname{code}^i s \, \rho as follows:

\operatorname{code}^i s \, \rho = \operatorname{code}^i_R \, e \, \rho

\operatorname{check}^i c_0 \, c_{k-1} \, B

\operatorname{A}_0: \operatorname{code}^i s_0 \, \rho

\operatorname{jump} D

\operatorname{jump} A_{k-1}

\operatorname{C}: \operatorname{Code}^i s_k \, \rho

\operatorname{jump} D
```

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that is, c_i + 1 = c_{i+1} for i = [0, k-1].
Define code^i s \rho as follows:
   code^i s \rho = code^i_R e \rho
                       check^i c_0 c_{k-1} B
                                                       B: \operatorname{jump} A_0
                A_0: \operatorname{code}^i s_0 \rho
                         jump D
                                                              jump A_{k-1}
                                                        C:
               A_{k-1}: code<sup>i</sup> s_{k-1} \rho
                         jump D
check<sup>i</sup> l u B checks if l \leq R_i < u holds and jumps accordingly.
```

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### Translation of the checki Macro

The macro *check*<sup>i</sup> l u B checks if  $l \le R_i < u$ . Let k = u - l.

- if  $l \leq R_i < u$  it jumps to  $B + R_i l$
- if  $R_i < l$  or  $R_i \ge u$  it jumps to C

```
B: \text{ jump } A_0
\vdots \qquad \vdots
\text{ jump } A_{k-1}
C:
```

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we define:

```
\begin{array}{lll} \operatorname{check}^{i} \operatorname{l} u \, B & = & \operatorname{loadc} \, R_{i+1} \, \underline{l} \\ & & \operatorname{geq} \, R_{i+2} \, R_{i} \, R_{i+1} \\ & \operatorname{jumpz} \, R_{i+2} \, \underline{E} \\ & \operatorname{sub} \, R_{i} \, R_{i+1} \\ & \operatorname{loadc} \, R_{i+1} \, k \\ & & \operatorname{geq} \, R_{i+2} \, R_{i} \, R_{i+1} \\ & \operatorname{jumpz} \, R_{i+2} \, D \\ & C : & \mathcal{B} + \mathcal{L} \end{array}
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```

Note: a jump jumpi  $R_i$  B with  $R_i = k$  winds up at C.

## Improvements for Jump Tables

This translation is only suitable for *certain* switch-statement.

- In case the table starts with 0 instead of  $\ell$  we don't need to subtract it from e before we use it as index
- if the value of e is guaranteed to be in the interval [l,u], we can omit check
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## **Improvements for Jump Tables**

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- if the value of e is guaranteed to be in the interval [l,u], we can omit check
- can we implement the **switch**-statement using an *L*-attributed system without symbolic labels?
  - difficult since B is unknown when check is translated
  - → use symbolic labels or basic blocks

### **General translation of switch-Statements**

In general, the values of the various cases may be far apart:

• generate an if-ladder, that is, a sequence of if-statements

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- one could generate several jump tables, one for each sets of consecutive cases
- an if cascade can be re-arranged by using information from profiling, so that paths executed more frequently require fewer tests

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### **Translation into Basic Blocks**

Problem: How do we connect the different basic blocks? Idea:

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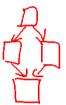
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Code Synthesis

**Chapter 5:** Functions

#### **Translation into Basic Blocks**

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- translation of a function: create an empty block and store a pointer to it in the node of the function declaration
- pass this block down to the translation of statements
- each new statement is appended to this basic block
- a two-way if-statement creates three new blocks:
  - one for the then-branch, connected with the current block by a jumpz-edge
  - one for the else-branch, connected with the current block by a jump-edge
  - one for the following statements, connect to the then- and else-branch by a jump edge
- similar for other constructs

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## **Ingredients of a Function**

The definition of a function consists of

- a name with which it can be called:
- a specification of its formal parameters;
- possibly a result type;
- a sequence of statements.

In C we have:

$$code_{R}^{i} f \rho = loadc f$$
 with  $f$  starting address of  $f$ 

#### Observe:

- function names must have an address assigned to them
- since the size of functions is unknown before they are translated, the addresses of forward-declared functions must be inserted later

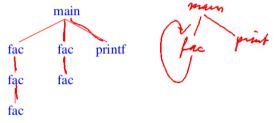
## **Memory Management in Functions**

```
int fac(int x) {
   if (x<=0) return 1;
   else return x*fac(x-1);
}

int main(void) {
   int n;
   n = fac(2) + fac(1);
   printf("%d", n);
}</pre>
```

At run-time several instance may be active, that is, the function has been called but has not yet returned.

The recursion tree in the example:



**Memory Management in Function Variables** 

The formal parameters and the local variables of the various (instances) of a function must be kept separate

Idea for implementing functions:

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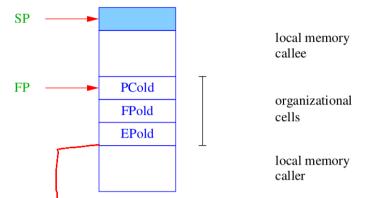
## **Memory Management in Function Variables**

The formal parameters and the local variables of the various (instances) of a function must be kept separate Idea for implementing functions:

- set up a region of memory each time it is called
- in sequential programs this memory region can be allocate on the stack
- thus, each instance of a function has its own region on the stack
- these regions are called stack frames)

## **Organization of a Stack Frame**

- stack representation: grows upwards
- SP points to the last used stack cell

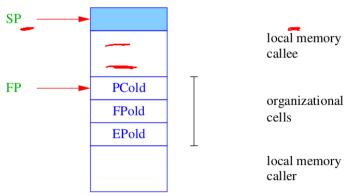


- FP  $\hat{=}$  frame pointer: points to the last organizational cell
- use to recover the previously active stack frame

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## **Organization of a Stack Frame**

- stack representation: grows upwards
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- FP = frame pointer: points to the last organizational cell
- use to recover the previously active stack frame
- EP has to do with the heap, will come to that later

## **Principle of Function Call and Return**

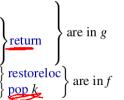
actions taken on entering g:

- 1. compute the start address of g
- 2. compute actual parameters
- 3. backup of caller-save registers
- 4. backup of FP, EP
- 5. set the new FP
- 6. back up of  $\overrightarrow{PC}$  and jump to the beginning of g
- 7. setup new EP
- 8. allocate space for local variables

actions taken on leaving g:

- 1. compute the result
- 2. restore FP, EP, SP
- return to the call site in f, that is, restore PC
- 4. restore the caller-save registers
- 5. clean up stack





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## **Managing Registers during Function Calls**

The two register sets (global and local) are used as follows:

- automatic variables live in *local* registers  $R_i$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$
- intermediate results also live in *local* registers R<sub>i</sub>
- parameters *global* registers  $R_i$  (with  $i \le 0$ )
- global variables:

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#### **Definition**

Let f be a function that calls g. A register  $R_i$  is called

- caller-saved if f backs up  $R_i$  and g may overwrite it
- *callee-saved* if  $f(R_i)$  does not back up g must restore it before it returns

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### **Translation of Function Calls**

A function call  $g(e_1, \dots e_n)$  is translated as follows:

$$\operatorname{code}_{R}^{i} \operatorname{g}(e_{1}, \dots e_{n}) \rho = \operatorname{code}_{R}^{i} \operatorname{g} \rho$$

$$\operatorname{code}_{R}^{i+1} e_{1} \rho$$

$$\vdots$$

$$\operatorname{code}_{R}^{i+n} e_{n} \rho$$

$$\operatorname{move} R_{-1} R_{i+1}$$

$$\vdots$$

$$\operatorname{move} R_{-n} R_{i+n}$$

$$\operatorname{saveloc} R_{1} R_{i-1}$$

$$\operatorname{mark}$$

$$\operatorname{call} R_{i}$$

$$\operatorname{call} R_{i}$$

$$\operatorname{prestoreloc} R_{1} R_{i-1}$$

$$\operatorname{move} R_{i} R_{0}$$

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#### New instructions:

- saveloc  $R_i$   $R_i$  pushes the registers  $R_i$ ,  $R_{i+1}$  ...  $R_i$  onto the stack
- mark backs up the organizational cells
- call  $R_i$  calls the function at the address in  $R_i$
- restoreloc  $R_i$   $R_j$  pops  $R_j$ ,  $R_{j-1}$ , ...  $R_i$  off the stack

### **Translation of Function Calls**

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$$\operatorname{code}_{R}^{i} g \rho$$

$$\operatorname{move} R_{-n} R_{i+n}$$

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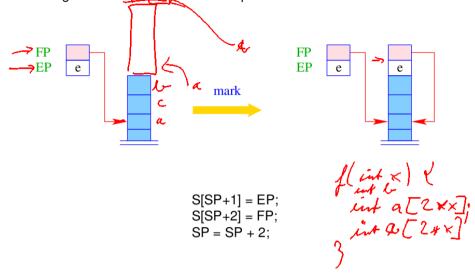
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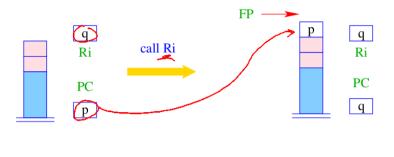
## Rescuing EP and FP

The instruction mark allocates stack space for the return value and the organizational cells and backs up FP and EP.



## **Calling a Function**

The instruction call rescues the value of PC+1 onto the stack and sets FP and PC.



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## **Result of a Function**

The global register set is also used to communicate the result value of a function:

$$\operatorname{code}^{i}\operatorname{return} e \rho = \operatorname{code}_{R}^{i} e \rho$$

$$\operatorname{move} R_{0} R_{i}$$

$$\operatorname{return}$$

## **Result of a Function**

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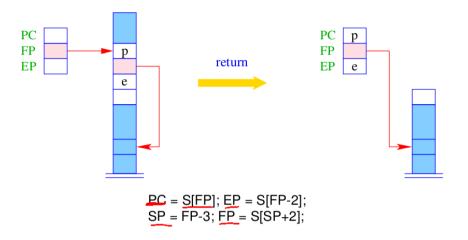
$$\operatorname{return}$$

alternative without result value:

$$code^i return \rho = return$$

## **Return from a Function**

The instruction return relinquishes control of the current stack frame, that is, it restores PC, EP and FP.



## **Translation of Functions**

The translation of a function is thus defined as follows:

$$\operatorname{code} \bigcap_{r} f(\operatorname{args}) \{ \operatorname{decls} \operatorname{ss} \} \rho = \operatorname{enter} q \\ \operatorname{move} \underbrace{R_{l+1} R_{-1}}_{\text{inversion}} \\ \operatorname{move} \underbrace{R_{l+n} R_{-n}}_{\operatorname{code}^{l+n+1} \operatorname{ss} \rho'}$$

Assumptions:

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### **Translation of Functions**

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```
\operatorname{code}^{1} t_{r} \operatorname{f}(\operatorname{args}) \{\operatorname{decls} \operatorname{ss}\} \rho = \operatorname{enter} q \\ \operatorname{move} R_{l+1} R_{-1} \\ \vdots \\ \operatorname{move} R_{l+n} R_{-n} \\ \operatorname{code}^{l+n+1} \operatorname{ss} \rho' \\ \operatorname{return}
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#### Assumptions:

• the function has *n* parameters

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### Assumptions:

- the function has *n* parameters
- the local variables are stored in registers  $R_1, \ldots R_l$
- the parameters of the function are in  $R_{-1}, \dots R_{-n}$

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- the function has n parameters
- the local variables are stored in registers  $R_1, \dots R_l$
- the parameters of the function are in  $R_{-1}, \dots R_{-n}$
- $\rho'$  is obtained by extending  $\rho$  with the bindings in decls and the function parameters args
- return is not always necessary

### Translation of Functions

The translation of a function is thus defined as follows:

```
\operatorname{code}^{1} t_{r} \, \operatorname{f}(\operatorname{args}) \{\operatorname{decls} \, \operatorname{ss}\} \, \rho \quad = \quad \operatorname{enter} q \\ \operatorname{move} R_{l+1} \, R_{-1} \\ \vdots \\ \operatorname{move} R_{l+n} \, R_{-n} \\ \operatorname{code}^{l+n+1} \operatorname{ss} \rho' \\ \operatorname{return}
```

#### Assumptions:

- the function has *n* parameters
- the local variables are stored in registers  $R_1, \dots R_l$
- the parameters of the function are in  $R_{-1}, \dots R_{-n}$
- $\rho'$  is obtained by extending  $\rho$  with the bindings in *decls* and the function parameters args

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## **Result of a Function**

The global register set is also used to communicate the result value of a function:

$$\operatorname{code}^{i}\operatorname{return} e \ 
ho = \operatorname{code}_{R}^{i} e \ 
ho$$

$$\operatorname{move} R_{0} R_{i}$$

$$\operatorname{return}$$

alternative without result value:

$$code^i$$
 return  $\rho$  = return

*global* registers are otherwise not used inside a function body:

- advantage: at any point in the body another function can be called without backing up *global* registers
- disadvantage: on entering a function, all global registers must be saved

## **Translation of Functions**

The translation of a function is thus defined as follows:

```
\operatorname{code}^{1} t_{r} \, \operatorname{f}(\operatorname{args}) \{\operatorname{decls} \, ss\} \, \rho = \operatorname{enter} q \\ \operatorname{move} R_{l+1} R_{-1} \\ \vdots \\ \operatorname{move} R_{l+n} R_{-n} \\ \operatorname{code}^{l+n+1} \operatorname{ss} \rho' \\ \operatorname{return}
```

#### Assumptions:

- the function has *n* parameters
- the local variables are stored in registers  $R_1, \ldots R_l$

## **Translation of Whole Programs**

A program  $P = F_1; \dots F_n$  must have a single main function.

```
\operatorname{code}^{1}P \rho = \operatorname{loadc} R_{1} \operatorname{\underline{\_main}}
\operatorname{mark}
\operatorname{call} R_{1}
\operatorname{\underline{\underline{halt}}}
f_{1} : \operatorname{code}^{1}F_{1} \rho \oplus \rho_{f_{1}}
\vdots
f_{n} : \operatorname{code}^{1}F_{n} \rho \oplus \rho_{f_{n}}
```

## **Translation of Whole Programs**

A program  $P = F_1; \dots F_n$  must have a single main function.

$$\operatorname{code}^1 P \rho = \operatorname{loadc} R_1 \operatorname{\_main}$$
 $\operatorname{mark}$ 
 $\operatorname{call} R_1$ 
 $\operatorname{halt}$ 
 $f_1 : \operatorname{code}^1 F_1 \rho \oplus \rho_{f_1}$ 
 $\vdots$ 
 $f_n : \operatorname{code}^1 F_n \rho \oplus \rho_{f_n}$ 

#### Assumptions:

- $\rho = \emptyset$  assuming that we have no global variables
- ullet  $\rho_{f_i}$  contain the addresses the local variables
- $\rho_1 \oplus \rho_2 = \lambda x \cdot \begin{cases} \rho_2(x) & \text{if } x \in \text{dom}(\rho_2) \\ \rho_1(x) & \text{otherwise} \end{cases}$

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## Translation of the fac-function

Consider:

```
int fac(int x) {
                                                move R_2 R_1
                                                                   x*fac(x-1)
 if (x \le 0) then
                                       i = 3 move R_3 R_1
                                                                   x-1
    return 1;
                                       i = 4 loadc R_4 1
                                                \operatorname{sub} R_3 R_3 R_4
    return x*fac(x-1);
                                       i = 3 move R_{-1} R_3
                                                                   fac(x-1)
                                                loadc R<sub>3</sub> _fac
                                                saveloc R_1 R_2
                         3 mark+call
  fac: enter 5
                                                mark
         move R_1 R_{-1} save param.
                                                call R<sub>3</sub>
 i = 2 move R_2 \overline{R_1}
                         if (x <= 0)
                                               restoreloc R_1 R_2
         loadc R_3 0
                                                move R_3 \overline{R_0}
         leq R_2 R_2 R_3
                                                mul \overline{R_2} R_2 R_3
         jumpz R_2 A
                         to else
                                                move R_0 R_2
                                                                   return x*..
         loadc R_2 1
                         return 1
                                                return
         move R_0 R_2
                                                return
         return
                         code is dead
         jump _B
```