

Script generated by TTT

Title: Petter: Compiler Construction (23.04.2020)
- 03: Finite Automata

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Chapter 2:
Basics: Finite Automata

Finite Automata

Definition Finite Automata

A **non-deterministic** finite automaton (NFA) is a tuple $A = (Q, \Sigma, \delta, I, F)$ with:

- Q a finite set of states;
- Σ a finite alphabet of inputs;
- $I \subseteq Q$ the set of start states;
- $F \subseteq Q$ the set of final states and
- δ the set of transitions (-relation)



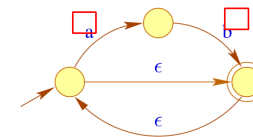
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Finite Automata

- Computations are paths in the graph.
- Accepting computations lead from I to F .
- An **accepted word** is the sequence of lables along an accepting computation ...



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Finite Automata

Once again, more formally:

- We define the **transitive closure** δ^* of δ as the smallest set δ' with:

$$\begin{aligned} & (p, \epsilon, p) \in \delta' \quad \text{and} \\ & (q, xw, q) \in \delta' \quad \text{if} \quad (p, x, p_1) \in \delta \quad \text{and} \quad (p_1, w, q) \in \delta' \end{aligned}$$

δ^* characterizes for a path between the states p and q the words obtained by concatenating the labels along it.

- The set of all accepting words, i.e. A 's **accepted language** can be described compactly as:

$$\mathcal{L}(A) = \{w \in \Sigma^* \mid \exists i \in I, f \in F : (i, w, f) \in \delta^*\}$$

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